

# Package ‘nmw’

March 14, 2017

**Version** 0.1.1

**Title** Understanding Nonlinear Mixed Effects Modeling for Population Pharmacokinetics

**Description** This shows how NONMEM(R) <<http://www.iconplc.com/innovation/nonmem/>> software works. NONMEM's classical estimation methods like 'First Order(FO) approximation', 'First Order Conditional Estimation(FOCE)', and 'Laplacian approximation' are explained.

**Depends** R (>= 3.0.0)

**ByteCompile** yes

**License** GPL-3

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**URL** <http://optimizer.r-forge.r-project.org/>

**NeedsCompilation** no

**Repository**

**Date** 2017-03-14

## R topics documented:

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## Description

This shows how NONMEM(R) <<http://www.iconplc.com/innovation/nonmem/>> software works.

## Details

This package explains 'First Order(FO) approximation' method, 'First Order Conditional Estimation(FOCE)' method, and 'Laplacian(LAPL)' method of NONMEM software.

## Author(s)

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## References

NONMEM Users guide

## Examples

```
DataAll = Theoph
colnames(DataAll) = c("ID", "BWT", "DOSE", "TIME", "DV")
DataAll[, "ID"] = as.numeric(as.character(DataAll[, "ID"]))

nTheta = 3
nEta = 3
nEps = 2

THETAinit = c(2, 50, 0.1) # Initial estimate
OMinit = matrix(c(0.2, 0.1, 0.1, 0.1, 0.2, 0.1, 0.1, 0.1, 0.2), nrow=nEta, ncol=nEta)
OMinit
SGinit = matrix(c(0.1, 0, 0, 0.1), nrow=nEps, ncol=nEps)
SGinit

LB = rep(0, nTheta) # Lower bound
UB = rep(1000000, nTheta) # Upper bound

PRED = function(THETA, ETA, DATAi) # Prediction function
{
  DOSE = 320
  TIME = DATAi[, "TIME"]

  KA = THETA[1]*exp(ETA[1])
  V = THETA[2]*exp(ETA[2])
  K = THETA[3]*exp(ETA[3])

  TERM1 = DOSE/V * KA/(KA - K)
  TERM2 = exp(-K*TIME)
  TERM3 = exp(-KA*TIME)

  F = TERM1 * (TERM2 - TERM3)
  G1 = -F*K/(KA - K) + KA*TIME*TERM1*TERM3
  G2 = -F
  G3 = (F/(KA - K) - TIME*TERM1*TERM2) * K
  H1 = F
  H2 = 1

  if (METHOD=="LAPL") {
    D11 = DOSE*(KA*V**-1.0*(-1.0*KA*(-2.0*KA*(-1.0*K+KA)**-3.0*(-1.0*TERM3+TERM2)+
      KA*TIME*TERM3*(-1.0*K+KA)**-2.0)+
      -1.0*KA*(-1.0*K+KA)**-2.0*(-1.0*TERM3+TERM2)+
      KA*TIME*(-1.0*KA*TIME*TERM3*(-1.0*K+KA)**-1.0+
```

```

-1.0*KA*TERM3*(-1.0*K+KA)**-2.0)+
KA*TIME*TERM3*(-1.0*K+KA)**-1.0)+
KA*V**-1.0*(-1.0*K+KA)**-1.0*(-1.0*TERM3+TERM2)+
2.0*KA*V**-1.0*(-1.0*KA*(-1.0*K+KA)**-2.0*(-1.0*TERM3+TERM2))+
KA*TIME*TERM3*(-1.0*K+KA)**-1.0))
D21 = -G1
D22 = F
D31 = DOSE*(KA*V**-1.0*(KA*K*TIME*TERM2*(-1.0*K+KA)**-2.0+
K*(-2.0*KA*(-1.0*K+KA)**-3.0*(-1.0*TERM3+TERM2))+
KA*TIME*TERM3*(-1.0*K+KA)**-2.0))+
KA*V**-1.0*(-1.0*K*TIME*TERM2*(-1.0*K+KA)**-1.0+
K*(-1.0*K+KA)**-2.0*(-1.0*TERM3+TERM2)))
D32 = -G3
D33 = DOSE*KA*V**-1.0*(-1.0*K*TIME*(-1.0*K*TIME*TERM2*(-1.0*K+KA)**-1.0+
K*TERM2*(-1.0*K+KA)**-2.0)+-1.0*K*TIME*TERM2*(-1.0*K+KA)**-1.0+
K*(-1.0*K*TIME*TERM2*(-1.0*K+KA)**-2.0+
2.0*K*(-1.0*K+KA)**-3.0*(-1.0*TERM3+TERM2)))+
K*(-1.0*K+KA)**-2.0*(-1.0*TERM3+TERM2))
} else {
  D11 = 0
  D21 = 0
  D22 = 0
  D31 = 0
  D32 = 0
  D33 = 0
}

return(cbind(F, G1, G2, G3, H1, H2, D11, D21, D22, D31, D32, D33))
}
#####
METHOD = "ZERO" # PRED function refers this.
InitStep(DataAll, THETAinit=THETAinit, OMinit=OMinit, SGinit=SGinit, nTheta=nTheta,
          LB=LB, UB=UB, METHOD=METHOD, Pred=PRED)
(EstRes = EstStep())          # It will take about 3 secs.
(CovRes = CovStep())          # It will take about 1 sec.
PostHocEta() # FinalPara from EstStep()

#####
#METHOD = "COND" # PRED function refers this.
#InitStep(DataAll, THETAinit=THETAinit, OMinit=OMinit, SGinit=SGinit, nTheta=nTheta,
#          LB=LB, UB=UB, METHOD=METHOD, Pred=PRED)
#(EstRes = EstStep())          # It will take about 4 mins.
#(CovRes = CovStep())          # It will take about 40 secs.
#get("EBE", envir=e)

##### "LAPL" usually fails due to numerical difficulties.
#METHOD = "LAPL" # PRED function refers this.
#THETAinit = c(4, 50, 0.2) # It is changed for better convergence.
#InitStep(DataAll, THETAinit=THETAinit, OMinit=OMinit, SGinit=SGinit, nTheta=nTheta,
#          LB=LB, UB=UB, METHOD=METHOD, Pred=PRED)
#(EstRes = EstStep())          # It will take about 3 mins. Succeeded with R-3.3.3 x64
#(CovRes = CovStep())          # It will take about 1 min.
#get("EBE", envir=e)

```

**Description**

It calculates standard errors and various variance matrices with the `e$FinalPara` after estimation step.

**Usage**

```
CovStep()
```

**Details**

Because `EstStep` uses nonlinear optimization, covariance step is separated from estimation step. It calculates variance-covariance matrix of estimates on the original scale.

**Value**

|  |  |
|--|--|
| Time                                   | consumed time  |
| Standard Error                         | standard error of the estimates in the order of theta, omega, and sigma  |
| Covariance Matrix of Estimates         | covariance matrix of estimates in the order of theta, omega, and sigma. This is $\text{inverse}(\mathbf{R}) \times \mathbf{S} \times \text{inverse}(\mathbf{R})$ by default. |
| Correlation Matrix of Estimates        | correlation matrix of estimates in the order of theta, omega, and sigma  |
| Inverse Covariance Matrix of Estimates | inverse covariance matrix of estimates in the order of theta, omega, and sigma   |
| Eigen Values                           | eigen values of covariance matrix  |
| R Matrix                               | R matrix of NONMEM, second derivative of log likelihood function with respect to estimation parameters   |
| S Matrix                               | S matrix of NONMEM, sum of individual cross-product of first derivative of log likelihood function with respect to estimation parameters                                     |

**Author(s)**

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**References**

NONMEM Users Guide

**See Also**

[EstStep](#), [InitStep](#)

**Examples**

```
# Only after InitStep and EstStep
#CovStep()
```

---

EstStep

*Estimation Step*


---

**Description**

This estimates upon the conditions with InitStep.

**Usage**

```
EstStep()
```

**Details**

It does not have arguments. All necessary arguments are stored in the `e` environment. It assumes "INTERACTION" between eta and epsilon for "COND" and "LAPL" options. The output is basically same with NONMEM output.

**Value**

|                 |                                       |
|-----------------|---------------------------------------|
| Initial OFV     | initial value of objective function   |
| Time            | time consumed for this step           |
| Optim           | the raw output from optim function    |
| Final Estimates | final estimates in the original scale |

**Author(s)**

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**References**

NONMEM Users Guide

**See Also**

[InitStep](#)

**Examples**

```
# Only After InitStep
#EstStep()
```

InitStep

*Initialization Step***Description**

It receives parameters for the estimation and stores them into the environment.

**Usage**

```
InitStep(DataAll, THETAinit, OMinit, SGinit, nTheta, LB = rep(0, nTheta),
        UB = rep(0, nTheta), Pred, METHOD = METHOD)
```

**Arguments**

|           |  |
|-----------|--|
| DataAll   | Data for all subjects. It should contain columns which Pred function uses. |
| THETAinit | Theta initial values   |
| OMinit    | Omega matrix initial values  |
| SGinit    | Sigma matrix initial values  |
| nTheta    | Number of thetas   |
| LB        | Lower bounds for theta vector  |
| UB        | Upper bounds for theta vector  |
| Pred      | Prediction function name   |
| METHOD    | one of the estimation methods "ZERO", "COND", "LAPL"                       |

**Details**

Prediction function should return not only prediction values (F or IPRED) but also G (first derivative with respect to  $\eta$ s) and H (first derivative of Y with respect to  $\epsilon$ ). For the "LAPL", prediction function should return second derivative with respect to  $\eta$  also. All objective functions assume NONMEM "INTERACTION" option for "COND" and "LAPL" option. Omega matrix should be full block one. Sigma matrix should be diagonal one.

**Value**

This does not return values, but stores necessary values into the environment `e`.

**Author(s)**

Kyun-Seop Bae <k@acr.kr>

**References**

NONMEM Users Guide

**Examples**

```

DataAll = Theoph
colnames(DataAll) = c("ID", "BWT", "DOSE", "TIME", "DV")
DataAll[, "ID"] = as.numeric(as.character(DataAll[, "ID"]))

nTheta = 3
nEta = 3
nEps = 2

THETAinit = c(2, 50, 0.1) # Initial estimate
OMinit = matrix(c(0.2, 0.1, 0.1, 0.1, 0.2, 0.1, 0.1, 0.1, 0.2), nrow=nEta, ncol=nEta)
OMinit
SGinit = matrix(c(0.1, 0, 0, 0.1), nrow=nEps, ncol=nEps)
SGinit

LB = rep(0, nTheta) # Lower bound
UB = rep(1000000, nTheta) # Upper bound

PRED = function(THETA, ETA, DATAi) # Prediction function
{
  DOSE = 320
  TIME = DATAi[, "TIME"]

  KA = THETA[1]*exp(ETA[1])
  V = THETA[2]*exp(ETA[2])
  K = THETA[3]*exp(ETA[3])

  TERM1 = DOSE/V * KA/(KA - K)
  TERM2 = exp(-K*TIME)
  TERM3 = exp(-KA*TIME)

  F = TERM1 * (TERM2 - TERM3)
  G1 = -F*K/(KA - K) + KA*TIME*TERM1*TERM3
  G2 = -F
  G3 = (F/(KA - K) - TIME*TERM1*TERM2) * K
  H1 = F
  H2 = 1

  if (METHOD=="LAPL") {
    D11 = DOSE*(KA*V**-1.0*(-1.0*KA*(-2.0*KA*(-1.0*K+KA)**-3.0*(-1.0*TERM3+TERM2)+
      KA*TIME*TERM3*(-1.0*K+KA)**-2.0)+
      -1.0*KA*(-1.0*K+KA)**-2.0*(-1.0*TERM3+TERM2)+
      KA*TIME*(-1.0*KA*TIME*TERM3*(-1.0*K+KA)**-1.0+
      -1.0*KA*TERM3*(-1.0*K+KA)**-2.0)+
      KA*TIME*TERM3*(-1.0*K+KA)**-1.0)+
      KA*V**-1.0*(-1.0*K+KA)**-1.0*(-1.0*TERM3+TERM2)+
      2.0*KA*V**-1.0*(-1.0*KA*(-1.0*K+KA)**-2.0*(-1.0*TERM3+TERM2)+
      KA*TIME*TERM3*(-1.0*K+KA)**-1.0))
    D21 = -G1
    D22 = F
    D31 = DOSE*(KA*V**-1.0*(KA*K*TIME*TERM2*(-1.0*K+KA)**-2.0+
      K*(-2.0*KA*(-1.0*K+KA)**-3.0*(-1.0*TERM3+TERM2)+
      KA*TIME*TERM3*(-1.0*K+KA)**-2.0))+
      KA*V**-1.0*(-1.0*K*TIME*TERM2*(-1.0*K+KA)**-1.0+
      K*(-1.0*K+KA)**-2.0*(-1.0*TERM3+TERM2)))
    D32 = -G3
  }
}

```

```

D33 = DOSE*KA*V**(-1.0*(-1.0*K*TIME*(-1.0*K*TIME*TERM2*(-1.0*K+KA)**-1.0+
K*TERM2*(-1.0*K+KA)**-2.0)+-1.0*K*TIME*TERM2*(-1.0*K+KA)**-1.0+
K*(-1.0*K*TIME*TERM2*(-1.0*K+KA)**-2.0+
2.0*K*(-1.0*K+KA)**-3.0*(-1.0*TERM3+TERM2)))+
K*(-1.0*K+KA)**-2.0*(-1.0*TERM3+TERM2))
} else {
  D11 = 0
  D21 = 0
  D22 = 0
  D31 = 0
  D32 = 0
  D33 = 0
}

return(cbind(F, G1, G2, G3, H1, H2, D11, D21, D22, D31, D32, D33))
}
#####
METHOD = "ZERO" # PRED function refers this.
InitStep(DataAll, THETAinit=THETAinit, OMinit=OMinit, SGinit=SGinit, nTheta=nTheta,
         LB=LB, UB=UB, METHOD=METHOD, Pred=PRED)

##### OR
METHOD = "COND" # PRED function refers this.
InitStep(DataAll, THETAinit=THETAinit, OMinit=OMinit, SGinit=SGinit, nTheta=nTheta,
         LB=LB, UB=UB, METHOD=METHOD, Pred=PRED)

##### OR
METHOD = "LAPL" # PRED function refers this.
THETAinit = c(4, 50, 0.2) # It is changed for better convergence for Theoph example.
InitStep(DataAll, THETAinit=THETAinit, OMinit=OMinit, SGinit=SGinit, nTheta=nTheta,
         LB=LB, UB=UB, METHOD=METHOD, Pred=PRED)

```



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