

Package ‘BFF’

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Title Bayes Factor Functions

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Description

Bayes factors represent the ratio of probabilities assigned to data by competing scientific hypotheses. However, one drawback of Bayes factors is their dependence on prior specifications that define null and alternative hypotheses. Additionally, there are challenges in their computation. To address these issues, we define Bayes factor functions (BFFs) directly from common test statistics. BFFs express Bayes factors as a function of the prior densities used to define the alternative hypotheses. These prior densities are centered on standardized effects, which serve as indices for the BFF. Therefore, BFFs offer a summary of evidence in favor of alternative hypotheses that correspond to a range of scientifically interesting effect sizes. Such summaries remove the need for arbitrary thresholds to determine “statistical significance.” BFFs are available in closed form and can be easily computed from z, t, chi-squared, and F statistics. They depend on hyperparameters “r” and “tau^2”, which determine the shape and scale of the prior distributions defining the alternative hypotheses. For replicated designs, the “r” parameter in each function can be adjusted to be greater than 1. Plots of BFFs versus effect size provide informative summaries of hypothesis tests that can be easily aggregated across studies.

License GPL (>= 2)

Encoding UTF-8

Imports BSDA, grDevices, graphics, hypergeo, ggplot2, Matrix, gsl,
stats

Suggests testthat (>= 2.1.0), knitr, rmarkdown

RoxygenNote 7.2.3

VignetteBuilder knitr

Depends R (>= 2.10)

NeedsCompilation no

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R topics documented:

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| chi2_test_BFF | <i>chi2_test_BFF</i> |
|---------------|----------------------|

Description

chi2_test_BFF constructs BFFs based on the chi-squared test. BFFs depend on hyperparameters r and τ^2 which determine the shape and scale of the prior distributions which define the alternative hypotheses. By setting $r > 1$, we use higher-order moments for replicated studies. Fractional moments are set with $r > 1$ and r not an integer. All results are on the log scale. Plot saved to working directory unless a full path is specified in the 'savename' variable of the function.

Usage

```
chi2_test_BFF(
  chi2_stat,
  n = NULL,
  df = NULL,
  pearsons = TRUE,
  savename = NULL,
  maximize = FALSE,
  r = 1,
  tau2 = NULL,
  save = TRUE,
  xlab = NULL,
  ylab = NULL,
  main = NULL
)
```

Arguments

| | |
|-----------|---|
| chi2_stat | chi ² statistic |
| n | sample size |
| df | degrees of freedom |
| pearsons | Is this a test of Pearson's chi ² test for goodness-of-fit? Default is TRUE. FALSE assumes a likelihood ratio test |

| | |
|----------|--|
| savename | optional, filename for saving the pdf of the final plot |
| maximize | Should the value of r be maximized? Default is FALSE. Only set to TRUE if analyzing multiple studies |
| r | r value |
| tau2 | tau2 values (can be a single entry or a vector of values) |
| save | should a copy of the plot be saved? |
| xlab | optional, x label for plot |
| ylab | optional, y label for plot |
| main | optional, main label for plot |

Value

Returns Bayes factor function results

| | |
|--------------|---|
| BFF | The log of the Bayes Factor Function values |
| effect_size | Effect sizes tested (seq(0, 1, by = 0.01)) |
| BFF_max_RMSE | Maximum BFF value |
| max_RMSE | Effect size that maximizes BFF |
| tau2 | tau ² values tested |

Examples

```
chi2BFF = chi2_test_BFF(chi2_stat = 2.5, n = 50, df = 49, save = FALSE)
chi2BFF = chi2_test_BFF(chi2_stat = 2.5, n = 50, df = 49, save = FALSE, tau2 = 0.5)
chi2BFF = chi2_test_BFF(chi2_stat = 2.5, n = 50, df = 49, save = FALSE, tau2 = c(0.5, 0.8))
chi2_test_BFF(chi2_stat = 2.5, n = 50, df = 49, pearsons = FALSE, save = FALSE)
chi2_test_BFF(chi2_stat = 2.5, n = 50, df = 49, r = 2, save = FALSE)
chi2_test_BFF(chi2_stat = 2.5, n = 50, df = 49, r = 2, pearsons = FALSE, save = FALSE)
chi2_test_BFF(chi2_stat = 2.5, n = 50, df = 49, r = 2.5, save = FALSE)
chi2_test_BFF(chi2_stat = 2.5, n = 50, df = 49, r = 2.5, pearsons = FALSE, save = FALSE)
chi2_test_BFF(chi2_stat=2.5, n = 50, df = 49, maximize = TRUE)
chi2_test_BFF(chi2_stat=2.5, n = 50, df = 49, maximize = TRUE, tau2 = 0.5)
chi2_test_BFF(chi2_stat=2.5, n = 50, df = 49, maximize = TRUE, tau2 = c(0.5, 0.8))
chi2BFF$BFF_max_RMSE # maximum BFF value
chi2BFF$max_RMSE    # effect size which maximizes the BFF
```

Description

f_test_BFF constructs BFFs based on the F test. BFFs depend on hyperparameters r and τ^2 which determine the shape and scale of the prior distributions which define the alternative hypotheses. By setting $r > 1$, we use higher-order moments for replicated studies. Fractional moments are set with $r > 1$ and r not an integer. All results are on the log scale. Plot saved to working directory unless a full path is specified in the 'savename' variable of the function.

Usage

```
f_test_BFF(
  f_stat,
  n,
  df1,
  df2,
  savename = NULL,
  maximize = FALSE,
  r = 1,
  tau2 = NULL,
  save = TRUE,
  xlab = NULL,
  ylab = NULL,
  main = NULL
)
```

Arguments

| | |
|----------|---|
| f_stat | F statistic |
| n | sample size |
| df1 | first degree of freedom |
| df2 | first degree of freedom |
| savename | optional, filename for saving the pdf of the final plot |
| maximize | should the function be maximized over all possible r values? Default is FALSE. Only set to TRUE if analyzing multiple studies |
| r | r value |
| tau2 | τ^2 values (can be a single entry or a vector of values) |
| save | should a copy of the plot be saved? |
| xlab | optional, x label for plot |
| ylab | optional, y label for plot |
| main | optional, main label for plot |

Value

Returns Bayes factor function results

| | |
|-----|---|
| BFF | The log of the Bayes Factor Function values |
|-----|---|

| | |
|--------------|--|
| effect_size | Effect sizes tested (seq(0, 1, by = 0.01)) |
| BFF_max_RMSE | Maximum BFF value |
| max_RMSE | Effect size that maximizes BFF |
| tau2 | tau^2 values tested |

Examples

```
fBFF = f_test_BFF(f_stat = 2.5, n = 50, df1 = 20, df2 = 48, save = FALSE)
f_test_BFF(f_stat = 2.5, n = 50, df1 = 20, df2 = 48, save = FALSE, tau2 = 0.5)
f_test_BFF(f_stat = 2.5, n = 50, df1 = 20, df2 = 48, save = FALSE, tau2 = c(0.5, 0.8))
f_test_BFF(f_stat = 2.5, n = 50, df1 = 20, df2 = 48, r = 2, save = FALSE)
f_test_BFF(f_stat = 2.5, n = 50, df1 = 20, df2 = 48, r = 2.5, save = FALSE)
f_test_BFF(f_stat=2.5, n = 50, df1 = 20, df2 = 48, maximize = TRUE)
f_test_BFF(f_stat=2.5, n = 50, df1 = 20, df2 = 48, maximize = TRUE, tau2 = 0.5)
f_test_BFF(f_stat=2.5, n = 50, df1 = 20, df2 = 48, maximize = TRUE, tau2 = c(0.5, 0.8))
fBFF$BFF_max_RMSE # maximum BFF value
fBFF$max_RMSE     # effect size which maximizes the BFF value
```

t_test_BFF

t_test_BFF

Description

t_test_BFF constructs BFFs based on the t test. BFFs depend on hyperparameters r and τ^2 which determine the shape and scale of the prior distributions which define the alternative hypotheses. By setting $r > 1$, we use higher-order moments for replicated studies. Fractional moments are set with $r > 1$ and r not an integer. All results are on the log scale. Plot saved to working directory unless a full path is specified in the 'savename' variable of the function.

Usage

```
t_test_BFF(
  t_stat,
  n = NULL,
  df = NULL,
  one_sample = TRUE,
  n1 = NULL,
  n2 = NULL,
  savename = NULL,
  maximize = FALSE,
  r = 1,
  tau2 = NULL,
```

```

    save = TRUE,
    xlab = NULL,
    ylab = NULL,
    main = NULL
  )

```

Arguments

| | |
|------------|---|
| t_stat | T statistic |
| n | sample size (if one sample test) |
| df | degrees of freedom |
| one_sample | is test one sided? Default is TRUE |
| n1 | sample size of group one for two sample test |
| n2 | sample size of group two for two sample test |
| savename | optional, filename for saving the pdf of the final plot |
| maximize | should the function be maximized over all possible r values? Default is FALSE. Only set to TRUE if analyzing multiple studies |
| r | r value |
| tau2 | tau2 values (can be a single entry or a vector of values) |
| save | should a copy of the plot be saved? |
| xlab | optional, x label for plot |
| ylab | optional, y label for plot |
| main | optional, main label for plot |

Value

Returns Bayes factor function results

| | |
|--------------|---|
| BFF | The log of the Bayes Factor Function values |
| effect_size | Effect sizes tested (seq(0, 1, by = 0.01)) |
| BFF_max_RMSE | Maximum BFF value |
| max_RMSE | Effect size that maximizes BFF |
| tau2 | tau ² values tested |

Examples

```

tBFF = t_test_BFF(t_stat = 2.5, n = 50, df = 49, save = FALSE)
t_test_BFF(t_stat = 2.5, n = 50, df = 49, save = FALSE, tau2 = 0.5)
t_test_BFF(t_stat = 2.5, n = 50, df = 49, save = FALSE, tau2 = c(0.5, 0.2))
t_test_BFF(t_stat = 2.5, n1 = 50, n2 = 40, df = 88, save = FALSE, one_sample = FALSE)

```

```

t_test_BFF(t_stat = 2.5, n = 50, r = 2, df = 49, save = FALSE)
t_test_BFF(t_stat = 2.5, r = 2, n1 = 50, n2 = 30, df = 78, one_sample = FALSE, save = FALSE)
t_test_BFF(t_stat = 2.5, n = 50, r = 2.5, df = 49, save = FALSE)
t_test_BFF(t_stat=2.5, r = 2.5, n1 = 50, n2 = 30, df = 78, one_sample = FALSE, save=FALSE)
t_test_BFF(t_stat = 2.5, n = 50, df = 49, save = FALSE, maximize = TRUE)
t_test_BFF(t_stat = 2.5, n = 50, df = 49, save = FALSE, maximize = TRUE, tau2 = 0.5)
t_test_BFF(t_stat = 2.5, n = 50, df = 49, save = FALSE, maximize = TRUE, tau2 = c(0.5, 0.8))
tBFF$BFF_max_RMSE # maximum BFF value
tBFF$max_RMSE     # effect size which maximizes the BFF value

```

z_test_BFF

z_test_BFF

Description

z_test_BFF constructs BFFs based on the z test. BFFs depend on hyperparameters r and τ^2 which determine the shape and scale of the prior distributions which define the alternative hypotheses. By setting $r > 1$, we use higher-order moments for replicated studies. Fractional moments are set with $r > 1$ and r not an integer. All results are on the log scale. Plot saved to working directory unless a full path is specified in the 'savename' variable of the function.

Usage

```

z_test_BFF(
  z_stat,
  n = NULL,
  one_sample = TRUE,
  n1 = NULL,
  n2 = NULL,
  savename = NULL,
  maximize = FALSE,
  r = 1,
  tau2 = NULL,
  save = TRUE,
  xlab = NULL,
  ylab = NULL,
  main = NULL
)

```

Arguments

| | |
|------------|--|
| z_stat | z statistic |
| n | sample size (if one sample test) |
| one_sample | is test one sided? Default is TRUE |
| n1 | sample size of group one for two sample test |
| n2 | sample size of group two for two sample test |

| | |
|----------|--|
| savename | optional, filename for saving the pdf of the final plot |
| maximize | Should the value of r be maximized? Default is FALSE. Only set to TRUE if analyzing multiple studies |
| r | r value |
| tau2 | tau2 values (can be a single entry or a vector of values) |
| save | should a copy of the plot be saved? |
| xlab | optional, x label for plot |
| ylab | optional, y label for plot |
| main | optional, main label for plot |

Value

Returns Bayes factor function results

| | |
|--------------|---|
| BFF | The log of the Bayes Factor Function values |
| effect_size | Effect sizes tested (seq(0, 1, by = 0.01)) |
| BFF_max_RMSE | Maximum BFF value |
| max_RMSE | Effect size that maximizes BFF |
| tau2 | tau ² values tested |

Examples

```
zBFF = z_test_BFF(z_stat = 2.5, n = 50, save = FALSE)
z_test_BFF(z_stat = 2.5, n = 50, save = FALSE, tau2 = 0.5)
z_test_BFF(z_stat = 2.5, n = 50, save = FALSE, tau2 = c(0.5, 0.8))
z_test_BFF(z_stat = 2.5, n1 = 50, n2 = 35, one_sample = FALSE, save = FALSE) ##
z_test_BFF(z_stat = 2.5, n = 50, r = 2, save = FALSE)
z_test_BFF(z_stat = 2.5, r = 2, n1 = 50, n2 = 30, one_sample = FALSE, save = FALSE) ##
z_test_BFF(z_stat = 2.5, n = 50, r = 2.5, save = FALSE)
z_test_BFF(z_stat = 2.5, r = 2.5, n1 = 50, n2 = 30, one_sample = FALSE, save = FALSE) ##
z_test_BFF(z_stat=2.5, n = 50, maximize = TRUE)
z_test_BFF(z_stat=2.5, n = 50, maximize = TRUE, tau2 = 0.5)
z_test_BFF(z_stat=2.5, n = 50, maximize = TRUE, tau2 = c(0.5, 0.8))
zBFF$BFF_max_RMSE # maximum BFF value
zBFF$max_RMSE     # effect size which maximizes the BFF value
```


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