# Package 'exametrika'

November 22, 2024

Type Package

Title Test Theory Analysis and Biclustering

Version 1.1.0

Description Implements comprehensive test data engineering methods as described in Shojima (2022, ISBN:978-9811699856). Provides statistical techniques for engineering and processing test data: Classical Test Theory (CTT) with reliability coefficients for continuous ability assessment; Item Response Theory (IRT) including Rasch, 2PL, and 3PL models with item/test information functions; Latent Class Analysis (LCA) for nominal clustering; Latent Rank Analysis (LRA) for ordinal clustering with automatic determination of cluster numbers; Biclustering methods including infinite relational models for simultaneous clustering of examinees and items without predefined cluster numbers; and Bayesian Network Models (BNM) for visualizing inter-item dependencies. Features local dependence analysis through LRA and biclustering, parameter estimation, dimensionality assessment, and network structure visualization for educational, psychological, and social science research.

License MIT + file LICENSE

Language en-US

**Encoding** UTF-8

LazyData true

BuildVignettes true

RoxygenNote 7.3.2

**Suggests** testthat (>= 3.0.0)

Config/testthat/edition 3

**Depends** R (>= 3.5.0), mvtnorm, igraph

NeedsCompilation no

**Author** Koji Kosugi [aut, cre] (<a href="https://orcid.org/0000-0001-5816-0099">https://orcid.org/0000-0001-5816-0099</a>)

Maintainer Koji Kosugi <kosugitti@gmail.com>

Repository CRAN

**Date/Publication** 2024-11-22 09:30:02 UTC

2 Contents

# **Contents**

AlphaCoefficient	. 3
AlphaIfDel	
asymprior	. 5
Biclustering	
BINET	
Biserial Correlation	. 10
BitRespPtn	. 11
BNM	. 11
calcFitIndices	. 13
CCRR	. 13
crr	. 15
CTT	. 15
dataFormat	. 16
	. 10
dataFormat.long	
Dimensionality	. 19
FieldAnalysis	. 19
IIF2PLM	. 20
IIF3PLM	. 20
InterItemAnalysis	. 21
IRM	. 22
IRT	. 24
ITBiserial	. 26
ItemEntropy	. 27
ItemFit	. 28
ItemInformationFunc	. 29
ItemLift	. 29
ItemOdds	. 30
ItemStatistics	. 31
ItemThreshold	. 32
ItemTotalCorr	. 33
J12S5000	. 34
J15S500	. 35
J20S400	. 35
J35S515	. 36
J5S10	. 36
JCRR	. 37
JointSampleSize	. 38
LCA	
LDB	. 40
LDLRA	. 43
LD_param_est	. 45
LogisticModel	. 46
LRA	. 46
maxParents_penalty	. 48
MutualInformation	. 49
nrs	. 50

AlphaCoefficient 3

Index		<b>78</b>
	TwoPLM	76
	ThreePLM	
	TetrachoricCorrelationMatrix	
	tetrachoric	
	TestStatistics	
	TestInformationFunc	
	TestFitSaturated	
	TestFit	
	StudentAnalysis	69
	StrLearningPBIL_LDLRA	
	StrLearningPBIL_BNM	
	StrLearningGA_BNM	
	stanine	
	sscore	60
	softmax	60
	slopeprior	<b>5</b> 9
	RaschModel	
	PSD_item_params	58
	print.exametrika	
	plot.exametrika	
	PhiCoefficient	
	percentile	
	passage	
	OmegaCoefficient	
	objective_function_IRT	51

AlphaCoefficient

Alpha Coefficient

# Description

This function computes Tau-Equivalent Measurement, also known as Cronbach's alpha coefficient, for a given data set.

### Usage

```
AlphaCoefficient(x, na = NULL, Z = NULL, w = NULL)
```

# Arguments

X	This should be a data matrix or a Covariance/Phi/Tetrachoric matrix.
na	This parameter identifies the numbers or characters that should be treated as missing values when 'x' is a data matrix.
Z	This parameter represents a missing indicator matrix. It is only needed if 'x' is a data matrix.
W	This parameter is an item weight vector. It is only required if 'x' is a data matrix.

4 AlphaIfDel

#### Value

For a correlation/covariance matrix input, returns a single numeric value representing the alpha coefficient. For a data matrix input, returns a list with three components:

- AlphaCov: Alpha coefficient calculated from covariance matrix
- AlphaPhi: Alpha coefficient calculated from phi coefficient matrix
- AlphaTetrachoric: Alpha coefficient calculated from tetrachoric correlation matrix

### References

Cronbach, L. J. (1951). Coefficient alpha and the internal structure of a test. Psychometrika, 16,297–334.

AlphaIfDel

Alpha Coefficient if Item removed

### Description

This function returns the alpha coefficient when the specified item is excluded.

### Usage

```
AlphaIfDel(x, delItem = NULL, na = NULL, Z = NULL, w = NULL)
```

#### **Arguments**

Χ	This should be a data matrix or a Covariance/Phi/Tetrachoric matrix.
delI	em Specify the item to be deleted. If NULL, calculations are performed for all cases.
na	This parameter identifies the numbers or characters that should be treated as missing values when 'x' is a data matrix.
Z	This parameter represents a missing indicator matrix. It is only needed if 'x' is a data matrix.
W	This parameter is an item weight vector. It is only required if 'x' is a data matrix.

asymprior 5

asymprior

Prior distribution function with guessing parameter

# Description

Prior distribution function with guessing parameter

### Usage

```
asymprior(c, alp, bet)
```

## Arguments

c guessing parameter
alp prior to be set
bet prior to be set

Biclustering

Biclustering and Ranklustering

### Description

performs biclustering, rankclustering, and their confirmatory models.

### Usage

```
Biclustering(
U,
ncls = 2,
nfld = 2,
Z = NULL,
w = NULL,
na = NULL,
method = "B",
conf = NULL,
mic = FALSE,
maxiter = 100,
verbose = TRUE
)
```

6 Biclustering

#### **Arguments**

U is either a data class of exametrika, or raw data. When raw data is given, it is

converted to the exametrika class with the dataFormat function.

ncls number of classes nfld number of fields

Z is a missing indicator matrix of the type matrix or data.frame

w is item weight vector

na argument specifies the numbers or characters to be treated as missing values.

method One of:

"B": Biclustering "R": Ranklustering

conf For the confirmatory parameter, you can input either a vector with items and

corresponding fields in sequence, or a field membership profile matrix. In the case of the former, the field membership profile matrix will be generated internally. When providing a membership profile matrix, it needs to be either matrix or data.frame. The number of fields(nfld) will be overwrite to the number of columns of this matrix. The default is NULL, and the field membership matrix will be estimated according to the specified number of classes(ncls) and

fields(nfld).

mic Monotonic increasing IRP option. The default is FALSE.

maxiter Maximum number of iterations. default is 100.

verbose verbose output Flag. default is TRUE

#### Value

**nobs** Sample size. The number of rows in the dataset.

testlength Length of the test. The number of items included in the test.

Nclass number of classes you set

**BRM** Bicluster Reference Matrix

FRP Field Reference Profile

**FRPIndex** Index of FFP includes the item location parameters B and Beta, the slope parameters A and Alpha, and the monotonicity indices C and Gamma.

TRP Test Reference Profile

FMP Field Membership Profile

**Students** Class/Rank Membership Profile matrix. The s-th row vector of  $\hat{M}_R$ ,  $\hat{m}_R$ , is the rank membership profile of Student s, namely the posterior probability distribution representing the student's belonging to the respective latent classes. It also includes the rank with the maximum estimated membership probability, as well as the rank-up odds and rank-down odds.

**LRD** Latent Rank Distribution. see also plot.exametrika

LCD Latent Class Distribution. see also plot.exametrika

LFD Latent Field Distribution. see also plot.exametrika

**RMD** Rank Membership Distribution.

TestFitIndices Overall fit index for the test. See also TestFit

BINET 7

#### **Examples**

```
# Perform Biclustering with Binary method (B)
# Analyze data with 5 fields and 6 classes
Biclustering(J35S515, nfld = 5, ncls = 6, method = "B")

# Perform Biclustering with Rank method (R)
# Store results for further analysis and visualization
result.Ranklusteing <- Biclustering(J35S515, nfld = 5, ncls = 6, method = "R")

# Display the Bicluster Reference Matrix (BRM) as a heatmap
plot(result.Ranklusteing, type = "Array")

# Plot Field Reference Profiles (FRP) in a 2x3 grid
# Shows the probability patterns for each field
plot(result.Ranklusteing, type = "FRP", nc = 2, nr = 3)

# Plot Rank Membership Profiles (RMP) for students 1-9 in a 3x3 grid
# Shows the posterior probability distribution of rank membership for each student
plot(result.Ranklusteing, type = "RMP", students = 1:9, nc = 3, nr = 3)</pre>
```

**BINET** 

Bicluster Network Model

#### **Description**

Bicluster Network Model: BINET is a model that combines the Bayesian network model and Biclustering. BINET is very similar to LDB and LDR. The most significant difference is that in LDB, the nodes represent the fields, whereas in BINET, they represent the class. BINET explores the local dependency structure among latent classes at each latent field, where each field is a locus.

#### Usage

```
BINET(
U,
Z = NULL,
w = NULL,
na = NULL,
conf = NULL,
ncls = NULL,
nfld = NULL,
g_list = NULL,
adj_list = NULL,
adj_file = NULL,
verbose = FALSE
)
```

8 BINET

#### Arguments

U U is either a data class of exametrika, or raw data. When raw data is given, it is converted to the exametrika class with the dataFormat function. 7 Z is a missing indicator matrix of the type matrix or data.frame w is item weight vector w na argument specifies the numbers or characters to be treated as missing values. na conf For the confirmatory parameter, you can input either a vector with items and corresponding fields in sequence, or a field membership profile matrix. In the case of the former, the field membership profile matrix will be generated internally. When providing a membership profile matrix, it needs to be either matrix or data.frame. The number of fields(nfld) will be overwrite to the number of columns of this matrix. number of classes ncls nfld number of fields g\_list A list compiling graph-type objects for each rank/class. adj\_list A list compiling matrix-type adjacency matrices for each rank/class. adj\_file A file detailing the relationships of the graph for each rank/class, listed in the order of starting point, ending point, and rank(class). verbose verbose output Flag. default is TRUE

#### Value

**nobs** Sample size. The number of rows in the dataset.

testlength Length of the test. The number of items included in the test.

Nclass Optimal number of classes.

Nfield Optimal number of fields.

crr Correct Response Rate

ItemLabel Label of Items

FieldLabel Label of Fields

all\_adj Integrated Adjacency matrix used to plot graph.

all g Integrated graph object used to plot graph.see also plot.exametrika

adj\_list List of Adjacency matrix used in the model

params A list of the estimated conditional probabilities. It indicates which path was obtained from which parent node(class) to which child node(class), held by parent, child, and field. The item Items contained in the field is in fld. Named chap includes the conditional correct response answer rate of the child node, while pap contains the pass rate of the parent node.

**PSRP** Response pattern by the students belonging to the parent classes of Class c. A more comprehensible arrangement of params.

LCD Latent Class Distribution. see also plot.exametrika

**LFD** Latent Field Distribution. see also plot.exametrika

**CMD** Class Membership Distribution.

BINET 9

**FRP** Marginal bicluster reference matrix.

**FRPIndex** Index of FFP includes the item location parameters B and Beta, the slope parameters A and Alpha, and the monotonicity indices C and Gamma.

TRP Test Reference Profile

**LDPSR** A rearranged set of parameters for output. It includes the field the items contained within that field, and the conditional correct response rate of parent nodes(class) and child node(class).

**FieldEstimated** Given vector which correspondence between items and the fields.

**Students** Rank Membership Profile matrix. The s-th row vector of  $M_R$ ,  $\hat{m}_R$ , is the rank membership profile of Student s, namely the posterior probability distribution representing the student's belonging to the respective latent classes.

**NextStage** The next class that easiest for students to move to, its membership probability, class-up odds, and the field required for more.

MG\_FitIndices Multigroup as Null model. See also TestFit

SM FitIndices Saturated Model as Null model. See also TestFit

### **Examples**

```
# Example: Bicluster Network Model (BINET)
# BINET combines Bayesian network model and Biclustering to explore
# local dependency structure among latent classes at each field
# Create field configuration vector based on field assignments
conf <- c(
  1, 5, 5, 5, 9, 9, 6, 6, 6, 6, 2, 7, 7, 11, 11, 7, 7,
  12, 12, 12, 2, 2, 3, 3, 4, 4, 4, 8, 8, 12, 1, 1, 6, 10, 10
# Create edge data for network structure between classes
edges_data <- data.frame(</pre>
  "From Class (Parent) >>>" = c(
   1, 2, 3, 4, 5, 7, 2, 4, 6, 8, 10, 6, 6, 11, 8, 9, 12
  ),
  ">>> To Class (Child)" = c(
   2, 4, 5, 5, 6, 11, 3, 7, 9, 12, 12, 10, 8, 12, 12, 11, 13
  ),
  "At Field (Locus)" = c(
    1, 2, 2, 3, 4, 4, 5, 5, 5, 5, 5, 7, 8, 8, 9, 9, 12
  )
)
# Save edge data to temporary CSV file
tmp_file <- tempfile(fileext = ".csv")</pre>
write.csv(edges_data, file = tmp_file, row.names = FALSE)
# Fit Bicluster Network Model
result.BINET <- BINET(</pre>
  U = J35S515,
  ncls = 13, # Maximum class number from edges (13)
  nfld = 12, # Maximum field number from conf (12)
```

10 Biserial\_Correlation

```
conf = conf, # Field configuration vector
  adj_file = tmp_file # Path to the CSV file
)
# Clean up temporary file
unlink(tmp_file)
# Display model results
print(result.BINET)
# Visualize different aspects of the model
plot(result.BINET, type = "Array") # Show bicluster structure
plot(result.BINET, type = "TRP") # Test Response Profile
plot(result.BINET, type = "LRD") # Latent Rank Distribution
plot(result.BINET,
  type = "RMP", # Rank Membership Profiles
  students = 1:9, nc = 3, nr = 3
)
plot(result.BINET,
  type = "FRP", # Field Reference Profiles
  nc = 3, nr = 2
plot(result.BINET,
  type = "LDPSR", # Locally Dependent Passing Student Rates
  nc = 3, nr = 2
```

Biserial\_Correlation Biserial Correlation

### **Description**

A biserial correlation is a correlation between dichotomous-ordinal and continuous variables.

#### Usage

```
Biserial_Correlation(i, t)
```

#### **Arguments**

i is a dichotomous-ordinal variable (0/1). x and y can also be the other way

t is a continuous variable. x and y can also be the other way around.

#### Value

The biserial correlation coefficient between the two variables.

BitRespPtn 11

BitRespPtn

Binary pattern maker

### Description

Binary pattern maker

### Usage

```
BitRespPtn(n)
```

### **Arguments**

n

decimal numbers

#### **Details**

```
if n <- 1, return 0,1 if n <- 2, return 00,01,10,11 and so on.
```

#### Value

binary patterns

BNM

Bayesian Network Model

# Description

performs Bayesian Network Model with specified graph structure

# Usage

```
BNM(
   U,
   Z = NULL,
   w = NULL,
   na = NULL,
   g = NULL,
   adj_file = NULL,
   adj_matrix = NULL
)
```

12 BNM

### Arguments

U	U is either a data class of exametrika, or raw data. When raw data is given, it converted to the exametrika class with the dataFormat function.	
Z	Z is a missing indicator matrix of the type matrix or data.frame	
W	w is item weight vector	
na	na argument specifies the numbers or characters to be treated as missing values.	
g	Specify a graph object suitable for the igraph class.	
adj_file	specify CSV file where the graph structure is specified.	
adj_matrix	specify adjacency matrix.	

#### **Details**

This function performs a Bayesian network analysis on the relationships between items. This corresponds to Chapter 8 of the text. It uses the igraph package for graph visualization and checking the adjacency matrix. You need to provide either a graph object or a CSV file where the graph structure is specified.

#### Value

```
nobs Sample size. The number of rows in the dataset.
testlength Length of the test. The number of items included in the test.
crr correct response ratio
TestFitIndices Overall fit index for the test. See also TestFit
adj Adjacency matrix\
param Learned Parameters
CCRR_table Correct Response Rate tables
```

## Examples

```
# Create a Directed Acyclic Graph (DAG) structure for item relationships
# Each row represents a directed edge from one item to another
DAG <-
matrix(
    c(
        "Item01", "Item02", # Item01 influences Item02
        "Item02", "Item03", # Item02 influences Item03
        "Item02", "Item04", # Item02 influences Item04
        "Item03", "Item05", # Item03 influences Item05
        "Item04", "Item05" # Item04 influences Item05
    ),
    ncol = 2, byrow = TRUE
)
# Convert the DAG matrix to an igraph object for network analysis
g <- igraph::graph_from_data_frame(DAG)
g</pre>
```

calcFitIndices 13

```
# Create adjacency matrix from the graph
# Shows direct connections between items (1 for connection, 0 for no connection)
adj_mat <- as.matrix(igraph::as_adjacency_matrix(g))
print(adj_mat)

# Fit Bayesian Network Model using the specified adjacency matrix
# Analyzes probabilistic relationships between items based on the graph structure
result.BNM <- BNM(J5S10, adj_matrix = adj_mat)
result.BNM</pre>
```

calcFitIndices

calc Fit Indices

#### Description

A general function that returns the model fit indices.

#### Usage

```
calcFitIndices(chi_A, chi_B, df_A, df_B, nobs)
```

### Arguments

chi_A	chi-squares for this model
chi_B	chi-squares for compared model
df_A	degrees of freedom for this model
df_B	degrees of freedom for compared model
nobs	number of observations for Information criteria

#### Value

- **NFI** Normed Fit Index. Lager values closer to 1.0 indicate a better fit.
- RFI Relative Fit Index. Lager values closer to 1.0 indicate a better fit.
- **IFI** Incremental Fit Index. Lager values closer to 1.0 indicate a better fit.
- TLI Tucker-Lewis Index. Lager values closer to 1.0 indicate a better fit.
- **CFI** Comparative Fit Index. Lager values closer to 1.0 indicate a better fit.
- **RMSEA** Root Mean Square Error of Approximation. Smaller values closer to 0.0 indicate a better fit.
- AIC Akaike Information Criterion. A lower value indicates a better fit.
- CAIC Consistent AIC.A lower value indicates a better fit.
- BIC Bayesian Information Criterion. A lower value indicates a better fit.

14 CCRR

$\sim$	

Conditional Correct Response Rate

### **Description**

The conditional correct response rate (CCRR) represents the ratio of the students who passed Item C (consequent item) to those who passed Item A (antecedent item). This function is applicable only to binary response data.

### Usage

```
CCRR(U, na = NULL, Z = NULL, w = NULL, ...)
```

### Arguments

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

#### Value

A matrix of conditional correct response rates with exametrika class. Each element (i,j) represents the probability of correctly answering item j given that item i was answered correctly.

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

### **Examples**

```
# example code
# Calculate CCRR using sample dataset J5S10
CCRR(J5S10)
```

crr 15

crr

Correct Response Rate

### **Description**

The correct response rate (CRR) is one of the most basic and important statistics for item analysis. This is an index of item difficulty and a measure of how many students out of those who tried an item correctly responded to it. This function is applicable only to binary response data.

The CRR for each item is calculated as:

$$p_j = \frac{\sum_{i=1}^{n} z_{ij} u_{ij}}{\sum_{i=1}^{n} z_{ij}}$$

where  $z_{ij}$  is the missing indicator and  $u_{ij}$  is the response.

#### Usage

```
crr(U, na = NULL, Z = NULL, w = NULL, ...)
```

### **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
• • •	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

#### Value

A numeric vector of weighted correct response rates for each item. Values range from 0 to 1, where higher values indicate easier items (more students answered correctly).

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

# Examples

```
# Simple binary data
U <- matrix(c(1, 0, 1, 1, 0, 1), ncol = 2)
crr(U)
# using sample datasaet
crr(J15S500)</pre>
```

16 dataFormat

CTT

Classical Test Theory

#### **Description**

This function calculates the overall alpha and omega coefficients for the given data matrix. It also computes the alpha coefficient for each item, assuming that item is excluded.

#### Usage

```
CTT(U, na = NULL, Z = NULL, w = NULL)
```

### **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector

### Value

Returns a list of class c("exametrika", "CTT") containing two data frames:

- Reliability: A data frame with overall reliability coefficients (Alpha and Omega) calculated using different correlation matrices (Covariance, Phi, and Tetrachoric)
- ReliabilityExcludingItem: A data frame showing alpha coefficients when each item is excluded, calculated using different correlation matrices

#### **Examples**

```
# using sample dataset
CTT(J15S500)
```

dataFormat

dataFormat

#### **Description**

This function serves the role of formatting the data prior to the analysis.

### Usage

```
dataFormat(data, na = NULL, id = 1, Z = NULL, w = NULL)
```

dataFormat.long 17

#### Arguments

data	is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
id	id indicates the column number containing the examinee ID. The default is 1. If the answer pattern is contained in the first column, it is treated as if there is no ID vector.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector

#### Value

- U For binary response data. A matrix with rows representing the sample size and columns representing the number of items, where elements are either 0 or 1.  $u_{ij} = 1$  indicates that student i correctly answered item j, while  $u_{ij} = 0$  means that student i answered item j incorrectly. If the data contains NA values, any value can be filled in the matrix U, represented by the following missing value index matrix Z. However, in this function, -1 is assigned.
- **Q** For polytomous response data. A matrix with rows representing the sample size and columns representing the number of items, where elements are non-negative integers. When input data is in factor format, the factor levels are converted to consecutive integers starting from 1, and the original factor labels are stored in factor\_labels.
- **ID** The ID label given by the designated column or function.

**ItemLabel** The item names given by the provided column names or function.

- **Z** Missing indicator matrix.  $z_{ij} = 1$  indicates that item j is presented to Student i, while  $z_{ij} = 0$  indicates item j is NOT presented to Student i.
- w Item weight vector
- **response.type** Character string indicating the type of response data: "binary" for binary responses or "polytomous" for polytomous responses.
- **factor\_labels** List containing the original factor labels when polytomous responses are provided as factors. NULL if no factor data is present.
- **categories** Numeric vector containing the number of response categories for each item. For binary data, all elements are 2.

dataFormat.long	dataFormat for long-type data	

#### **Description**

A function to reshape long data into a dataset suitable for exametrika.

18 dataFormat.long

#### Usage

```
dataFormat.long(
  data,
  na = NULL,
  Sid = NULL,
  Qid = NULL,
  Resp = NULL,
  w = NULL,
  response.type = NULL)
```

### **Arguments**

data	is a data matrix of the type matrix or data.frame. This must contain at least three columns to identify the student, the item, and the response. Additionally, it can include a column for the weight of the items.
na	na argument specifies the numbers or characters to be treated as missing values.
Sid	Specify the column number containing the student ID label vector.
Qid	Specify the column number containing the Question label vector.
Resp	Specify the column number containing the Response value vector.
W	Specify the column number containing the weight vector.
response.type	type of response data: "binary" or "polytomous" (can be abbreviated as "poly"). If NULL, the type is automatically determined from the data.

#### Value

- U For binary response data. A matrix with rows representing the sample size and columns representing the number of items, where elements are either 0 or 1.  $u_{ij} = 1$  indicates that student i correctly answered item j, while  $u_{ij} = 0$  means that student i answered item j incorrectly.
- **Q** For polytomous response data. A matrix with rows representing the sample size and columns representing the number of items, where elements are non-negative integers. When input data is in factor format, the factor levels are converted to consecutive integers starting from 1, and the original factor labels are stored in factor\_labels.
- **ID** The ID label given by the designated column or function.

ItemLabel The item names given by the provided column names or function.

- **Z** Missing indicator matrix.  $z_{ij} = 1$  indicates that item j is presented to Student i, while  $z_{ij} = 0$  indicates item j is NOT presented to Student i.
- w Item weight vector
- **response.type** Character string indicating the type of response data: "binary" for binary responses or "polytomous" for polytomous responses.
- **factor\_labels** List containing the original factor labels when polytomous responses are provided as factors. NULL if no factor data is present.
- **categories** Numeric vector containing the number of response categories for each item. For binary data, all elements are 2.

Dimensionality 19

Dimensionality	Dimensionality	
----------------	----------------	--

### Description

The dimensionality is the number of components the test is measuring.

### Usage

```
Dimensionality(U, na = NULL, Z = NULL, w = NULL)
```

### **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector

#### Value

Returns a list of class c("exametrika", "Dimensionality") containing:

- Component: Sequence of component numbers
- Eigenvalue: Eigenvalues of the tetrachoric correlation matrix
- PerOfVar: Percentage of variance explained by each component
- CumOfPer: Cumulative percentage of variance explained

### Description

```
output for Field Analysis
```

# Usage

```
FieldAnalysis(x, digits = 4)
```

### Arguments

X	Biclustering Objects yielded by Biclustering Function	
digits	printed digits	

20 IIF3PLM

### Value

Returns a list of class c("exametrika", "Biclustering", "FieldAnalysis") containing:

**FieldAnalysisMatrix** A matrix showing field analysis results with rows representing items and columns showing:

• CRR: Correct Response Rate

• LFE: Latent Field Estimation

• Field1...FieldN: Field membership values

IIF2PLM

IIF for 2PLM

### Description

Item Information Function for 2PLM

### Usage

```
IIF2PLM(a, b, theta)
```

#### **Arguments**

a slope parameterb location parametertheta ability parameter

#### Value

Returns a numeric vector representing the item information at each ability level theta. The information is calculated as:  $I(\theta) = a^2 P(\theta) (1 - P(\theta))$ 

IIF3PLM

IIF for 3PLM

### **Description**

Item Information Function for 3PLM

### Usage

```
IIF3PLM(a, b, c, theta)
```

InterItemAnalysis 21

#### **Arguments**

a	slope parameter
b	location parameter
С	lower asymptote parameter
theta	ability parameter

#### Value

Returns a numeric vector representing the item information at each ability level theta. The information is calculated as:  $I(\theta) = \frac{a^2(1-P(\theta))(P(\theta)-c)^2}{(1-c)^2P(\theta)}$ 

 ${\tt InterItemAnalysis}$ 

Inter-Item Analysis

### **Description**

Inter-Item Analysis returns various metrics for analyzing relationships between pairs of items. This function is applicable only to binary response data. The following metrics are calculated:

• JSS: Joint Sample Size

• JCRR: Joint Correct Response Rate

• IL: Item Lift

• MI: Mutual Information

• Phi: Phi Coefficient

• Tetrachoric: Tetrachoric Correlation

Each metric is returned in matrix form where element (i,j) represents the relationship between items i and j.

### Usage

```
InterItemAnalysis(U, na = NULL, Z = NULL, w = NULL, ...)
```

# Arguments

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

IRM

#### Value

A list of class "exametrika" and "IIAnalysis" containing the following matrices:

JSS Joint Sample Size matrix

JCRR Joint Correct Response Rate matrix

IL Item Lift matrix

MI Mutual Information matrix

Phi Phi Coefficient matrix

**Tetrachoric** Tetrachoric Correlation matrix

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

### **Examples**

```
# example code
InterItemAnalysis(J15S500)
```

IRM

Infinite Relational Model

## Description

The purpose of this method is to find the optimal number of classes C, and optimal number of fields F. It can be found in a single run of the analysis, but it takes a long computation time when the sample size S is large. In addition, this method incorporates the Chinese restaurant process and Gibbs sampling. In detail, See Section 7.8 in Shojima(2022).

### Usage

```
IRM(
    U,
    Z = NULL,
    w = NULL,
    na = NULL,
    gamma_c = 1,
    gamma_f = 1,
    max_iter = 100,
    stable_limit = 5,
    minSize = 20,
    EM_limit = 20,
    seed = 123,
    verbose = TRUE
)
```

IRM 23

#### **Arguments**

U	U is either a data class of exametrika, or raw data. When raw data is given, it is converted to the exametrika class with the dataFormat function.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
na	na argument specifies the numbers or characters to be treated as missing values.
gamma_c	$\gamma_C$ is the hyperparameter of the CRP and represents the attractiveness of a new Class. As $\gamma_C$ increases, the student is more likely to be seated at a vacant class. The default is 1.
gamma_f	$\gamma_F$ is the hyperparameter of the CRP and represents the attractiveness of a new Field. The greater this value it more likely to be classified in the new field. The default is 1.
max_iter	A maximum iteration number of IRM process. The default is 100.
stable_limit	The IRM process exits the loop when the FRM stabilizes and no longer changes significantly. This option sets the maximum number of stable iterations, with a default of 5.
minSize	A value used for readjusting the number of classes. If the size of each class is less than minSize, the number of classes will be reduced. Note that this under limit of size is not used for either all correct or all incorrect class.
EM_limit	After IRM process, resizing the number of classes process will starts. This process using EM algorithm, EM_limit is the maximum number of iteration with default of 20.
seed	seed value for random numbers.
verbose	verbose output Flag. default is TRUE

#### Value

**nobs** Sample size. The number of rows in the dataset.

testlength Length of the test. The number of items included in the test.

Nclass Optimal number of classes.

**Nfield** Optimal number of fields.

**BRM** Bicluster Reference Matrix

FRP Field Reference Profile

**FRPIndex** Index of FFP includes the item location parameters B and Beta, the slope parameters A and Alpha, and the monotonicity indices C and Gamma.

TRP Test Reference Profile

FMP Field Membership Profile

**Students** Rank Membership Profile matrix. The s-th row vector of  $\hat{M}_R$ ,  $\hat{m}_R$ , is the rank membership profile of Student s, namely the posterior probability distribution representing the student's belonging to the respective latent classes. It also includes the rank with the maximum estimated membership probability, as well as the rank-up odds and rank-down odds.

LRD Latent Rank Distribution. see also plot.exametrika

24 IRT

**LFD** Latent Field Distribution. see also plot.exametrika

**RMD** Rank Membership Distribution.

TestFitIndices Overall fit index for the test. See also TestFit

#### **Examples**

```
# Fit an Infinite Relational Model (IRM) to determine optimal number of classes and fields
# gamma_c and gamma_f are concentration parameters for the Chinese Restaurant Process
result.IRM <- IRM(J35S515, gamma_c = 1, gamma_f = 1, verbose = TRUE)

# Display the Bicluster Reference Matrix (BRM) as a heatmap
# Shows the discovered clustering structure of items and students
plot(result.IRM, type = "Array")

# Plot Field Reference Profiles (FRP) in a 3-column grid
# Shows the probability patterns for each automatically determined field
plot(result.IRM, type = "FRP", nc = 3)

# Plot Test Reference Profile (TRP)
# Shows the overall response pattern across all fields
plot(result.IRM, type = "TRP")</pre>
```

IRT

Estimating Item parameters using EM algorithm

### **Description**

A function for estimating item parameters using the EM algorithm.

#### Usage

```
IRT(U, model = 2, na = NULL, Z = NULL, w = NULL, verbose = TRUE)
```

#### **Arguments**

U	U is either a data class of exametrika, or raw data. When raw data is given, it is converted to the exametrika class with the dataFormat function.
model	This argument takes the number of item parameters to be estimated in the logistic model. It is limited to values 2, 3, or 4.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
verbose	logical; if TRUE, shows progress of iterations (default: TRUE)

IRT 25

#### **Details**

Apply the 2, 3, and 4 parameter logistic models to estimate the item and subject populations. The 4PL model can be described as follows.

$$P(\theta, a_j, b_j, c_j, d_j) = c_j + \frac{d_j - c_j}{1 + exp\{-a_i(\theta - b_i)\}}$$

 $a_j, b_j, c_j$ , and  $d_j$  are parameters related to item j, and are parameters that adjust the logistic curve.  $a_j$  is called the slope parameter,  $b_j$  is the location,  $c_j$  is the lower asymptote, and  $d_j$  is the upper asymptote parameter. The model includes lower models, and among the 4PL models, the case where d=1 is the 3PL model, and among the 3PL models, the case where c=0 is the 2PL model.

#### Value

model number of item parameters you set.

testlength Length of the test. The number of items included in the test.

**nobs** Sample size. The number of rows in the dataset.

params Matrix containing the estimated item parameters

**Q3mat** Q3-matrix developed by Yen(1984)

itemPSD Posterior standard deviation of the item parameters

ability Estimated parameters of students ability

ItemFitIndices Fit index for each item. See also ItemFit

TestFitIndices Overall fit index for the test. See also TestFit

#### References

Yen, W. M. (1984) Applied Psychological Measurement, 8, 125-145.

#### **Examples**

```
# Fit a 3-parameter IRT model to the sample dataset
result.IRT <- IRT(J15S500, model = 3)

# Display the first few rows of estimated student abilities
head(result.IRT$ability)

# Plot Item Characteristic Curves (ICC) for items 1-6 in a 2x3 grid
plot(result.IRT, type = "ICC", items = 1:6, nc = 2, nr = 3)

# Plot Item Information Curves (IIC) for items 1-6 in a 2x3 grid
plot(result.IRT, type = "IIC", items = 1:6, nc = 2, nr = 3)

# Plot the Test Information Curve (TIC) for all items
plot(result.IRT, type = "TIC")</pre>
```

26 ITBiserial

|--|

### **Description**

The Item-Total Biserial Correlation computes the biserial correlation between each item and the total score. This function is applicable only to binary response data.

This correlation provides a measure of item discrimination, indicating how well each item distinguishes between high and low performing examinees.

## Usage

```
ITBiserial(U, na = NULL, Z = NULL, w = NULL, ...)
```

### **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

#### Value

A numeric vector of item-total biserial correlations. Values range from -1 to 1, where:

- Values near 1: Strong positive discrimination
- Values near 0: No discrimination
- Negative values: Potential item problems

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

The biserial correlation is generally preferred over the point-biserial correlation when the dichotomization is artificial (i.e., when the underlying trait is continuous).

### Examples

```
# using sample dataset
ITBiserial(J15S500)
```

ItemEntropy 27

ItemEntropy	Item Entropy	

#### **Description**

The item entropy is an indicator of the variability or randomness of the responses. This function is applicable only to binary response data.

The entropy value represents the uncertainty or information content of the response pattern for each item, measured in bits. Maximum entropy (1 bit) occurs when correct and incorrect responses are equally likely (p = 0.5).

#### Usage

```
ItemEntropy(U, na = NULL, Z = NULL, w = NULL, ...)
```

### Arguments

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
• • •	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

#### **Details**

The item entropy is calculated as:

$$e_j = -p_j \log_2 p_j - (1 - p_j) \log_2 (1 - p_j)$$

where  $p_i$  is the correct response rate for item j.

The entropy value has the following properties:

- Maximum value of 1 bit when p = 0.5 (most uncertainty)
- Minimum value of 0 bits when p = 0 or 1 (no uncertainty)
- Higher values indicate more balanced response patterns
- Lower values indicate more predictable response patterns

### Value

A numeric vector of entropy values for each item, measured in bits. Values range from 0 to 1, where:

- 1: maximum uncertainty (p = 0.5)
- 0: complete certainty (p = 0 or 1)
- Values near 1 indicate items with balanced response patterns
- Values near 0 indicate items with extreme response patterns

28 ItemFit

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

#### **Examples**

```
# using sample dataset
ItemEntropy(J5S10)
```

ItemFit

Model Fit Functions for Items

#### **Description**

A general function that returns the model fit indices.

### Usage

```
ItemFit(U, Z, ell_A, nparam)
```

### Arguments

U	U is either a data class of exametrika, or raw data. When raw data is given, it is converted to the exametrika class with the dataFormat function.
Z	Z is a missing indicator matrix of the type matrix or data.frame
ell_A	log likelihood of this model
nparam	number of parameters for this model

#### Value

model\_log\_like log likelihood of analysis model bench\_log\_like log likelihood of benchmark model null\_log\_like log likelihood of null model model\_Chi\_sq Chi-Square statistics for analysis model null\_Chi\_sq Chi-Square statistics for null model model\_df degrees of freedom of analysis model null\_df degrees of freedom of null model **NFI** Normed Fit Index. Lager values closer to 1.0 indicate a better fit. **RFI** Relative Fit Index. Lager values closer to 1.0 indicate a better fit.

**IFI** Incremental Fit Index. Lager values closer to 1.0 indicate a better fit.

TLI Tucker-Lewis Index. Lager values closer to 1.0 indicate a better fit.

CFI Comparative Fit Index. Lager values closer to 1.0 indicate a better fit.

ItemInformationFunc 29

**RMSEA** Root Mean Square Error of Approximation. Smaller values closer to 0.0 indicate a better fit.

AIC Akaike Information Criterion. A lower value indicates a better fit.

CAIC Consistent AIC.A lower value indicates a better fit.

BIC Bayesian Information Criterion. A lower value indicates a better fit.

ItemInformationFunc IIF for 4PLM

# Description

Item Information Function for 4PLM

### Usage

```
ItemInformationFunc(a = 1, b, c = 0, d = 1, theta)
```

### Arguments

a	slope parameter
b	location parameter
С	lower asymptote parameter
d	upper asymptote parameter
theta	ability parameter

### Value

Returns a numeric vector representing the item information at each ability level theta. The information is calculated based on the first derivative of the log-likelihood of the 4PL model with respect to theta.

ItemLift Item Lift

### **Description**

The lift is a commonly used index in a POS data analysis. The item lift of Item k to Item j is defined as follow:  $l_{jk} = \frac{p_{k|j}}{p_k}$  This function is applicable only to binary response data.

#### Usage

```
ItemLift(U, na = NULL, Z = NULL, w = NULL, ...)
```

30 ItemOdds

Argument	S
----------	---

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
• • •	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

#### Value

A matrix of item lift values with exametrika class. Each element (j,k) represents the lift value of item k given item j, which indicates how much more likely item k is to be correct given that item j was answered correctly.

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

#### References

Brin, S., Motwani, R., Ullman, J., & Tsur, S. (1997). Dynamic itemset counting and implication rules for market basket data. In Proceedings of ACM SIGMOD International Conference on Management of Data (pp. 255–264). https://dl.acm.org/doi/10.1145/253262.253325

#### **Examples**

```
# example code
# Calculate ItemLift using sample dataset J5S10
ItemLift(J5S10)
```

ItemOdds	Item Odds

#### **Description**

Item Odds are defined as the ratio of Correct Response Rate to Incorrect Response Rate:

$$O_j = \frac{p_j}{1 - p_j}$$

where  $p_j$  is the correct response rate for item j. This function is applicable only to binary response data.

The odds value represents how many times more likely a correct response is compared to an incorrect response. For example, an odds of 2 means students are twice as likely to answer correctly as incorrectly.

ItemStatistics 31

### Usage

```
ItemOdds(U, na = NULL, Z = NULL, w = NULL, ...)
```

### **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

#### Value

A numeric vector of odds values for each item. Values range from 0 to infinity, where:

- odds > 1: correct response more likely than incorrect
- odds = 1: equally likely
- odds < 1: incorrect response more likely than correct

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

### **Examples**

```
# using sample dataset
ItemOdds(J5S10)
```

ItemStatistics

Simple Item Statistics

# Description

This function calculates statistics for each item.

### Usage

```
ItemStatistics(U, na = NULL, Z = NULL, w = NULL)
```

### **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector

32 ItemThreshold

#### Value

**NR** Number of Respondents

**CRR** Correct Response Rate denoted as \$p\_j\$.

**ODDs** Item Odds is the ratio of the correct response rate to the incorrect response rate. Defined as  $o_j = \frac{p_j}{1-p_i}$ 

Threshold Item Threshold is a measure of difficulty based on a standard normal distribution.

**Entropy** Item Entropy is an indicator of the variability or randomness of the responses. Defined as  $e_j = -p_j \log_2 p_j - (1 - p_j) \log_2 (1 - p_j)$ 

**ITCrr** Item-total Correlation is a Pearson's correlation fo an item with the number of Number-Right score.

### **Examples**

```
# using sample dataset
ItemStatistics(J15S500)
```

ItemThreshold

Item Threshold

### **Description**

Item threshold is a measure of difficulty based on a standard normal distribution. This function is applicable only to binary response data.

The threshold is calculated as:

$$\tau_j = \Phi^{-1}(1 - p_j)$$

where  $\Phi^{-1}$  is the inverse standard normal distribution function and  $p_j$  is the correct response rate for item j.

Higher threshold values indicate more difficult items, as they represent the point on the standard normal scale above which examinees tend to answer incorrectly.

### Usage

```
ItemThreshold(U, na = NULL, Z = NULL, w = NULL, ...)
```

#### **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
	Internal personators for maintaining compatibility with the kinery data process

Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

ItemTotalCorr 33

### Value

A numeric vector of threshold values for each item on the standard normal scale. Typical values range from about -3 to 3, where:

- · Positive values indicate difficult items
- Zero indicates items of medium difficulty (50% correct)
- Negative values indicate easy items

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

### **Examples**

```
# using sample dataset
ItemThreshold(J5S10)
```

ItemTotalCorr

Item-Total Correlation

### **Description**

Item-Total correlation (ITC) is a Pearson's correlation of an item with the Number-Right Score (NRS) or total score. This function is applicable only to binary response data.

The ITC is a measure of item discrimination, indicating how well an item distinguishes between high and low performing examinees.

### Usage

```
ItemTotalCorr(U, na = NULL, Z = NULL, w = NULL, ...)
```

### **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

34 J12S5000

#### **Details**

The correlation is calculated between:

- Each item's responses (0 or 1)
- The total test score (sum of correct responses)

Higher positive correlations indicate items that better discriminate between high and low ability examinees.

#### Value

A numeric vector of item-total correlations. Values typically range from -1 to 1, where:

- Values near 1: Strong positive discrimination
- Values near 0: No discrimination
- Negative values: Potential item problems (lower ability students performing better than higher ability students)

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

Values below 0.2 might indicate problematic items that should be reviewed. Values above 0.3 are generally considered acceptable.

### **Examples**

```
# using sample dataset
ItemTotalCorr(J15S500)
```

J12S5000

J12S5000.Rdata

#### **Description**

J12S5000.Rdata

### Usage

J12S5000

#### Format

A data frame with 5000 students and 12 items

#### **Source**

http://shojima.starfree.jp/tde/index.htm

J15S500 35

J15S500

J15S500.Rdata

# Description

J15S500.Rdata

### Usage

J15S500

### **Format**

A data frame with 500 students and 15 items

### Source

http://shojima.starfree.jp/tde/index.htm

J20S400

J20S400.Rdata

# Description

J20S400.Rdata

### Usage

J20S400

### **Format**

A data frame with 400 students and 20 items

### Source

http://shojima.starfree.jp/tde/index.htm

*J5S10* 

J35S515

J35S515.Rdata

# Description

J35S515.Rdata

### Usage

J35S515

### **Format**

A data frame with 515 students and 35 items

### Source

http://shojima.starfree.jp/tde/index.htm

J5S10

J5S10.Rdata

# Description

J5S10.Rdata

### Usage

J5S10

### **Format**

A data frame with 5 students and 10 items

### Source

http://shojima.starfree.jp/tde/index.htm

JCRR 37

# Description

The joint correct response rate (JCRR) is the rate of students who passed both items. This function is applicable only to binary response data.

# Usage

```
JCRR(U, na = NULL, Z = NULL, w = NULL, ...)
```

# **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
w	w is item weight vector
	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

# Value

A matrix of joint correct response rates with exametrika class. Each element (i,j) represents the proportion of students who correctly answered both items i and j.

# Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

```
# example code
# Calculate JCRR using sample dataset J5S10
JCRR(J5S10)
```

38 LCA

JointSampleSize Join	nt Sample Size
----------------------	----------------

# Description

The joint sample size is a matrix whose elements are the number of individuals who responded to each pair of items.

# Usage

```
JointSampleSize(U, na = NULL, Z = NULL, w = NULL, ...)
```

# **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

#### Value

Returns a matrix of class c("exametrika", "matrix") where each element (i,j) represents the number of students who responded to both item i and item j. The diagonal elements represent the total number of responses for each item.

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

LCA	Latent Class Analysis	

# Description

A function for estimating LCA using the EM algorithm.

# Usage

```
LCA(U, ncls = 2, na = NULL, Z = NULL, w = NULL, maxiter = 100)
```

LCA 39

## **Arguments**

U	U is either a data class of exametrika, or raw data. When raw data is given, it is converted to the exametrika class with the dataFormat function.
ncls	number of latent class
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
maxiter	Maximum number of iterations.

#### Value

**nobs** Sample size. The number of rows in the dataset.

testlength Length of the test. The number of items included in the test.

Nclass number of classes you set

**TRP** Test Reference Profile matrix. The TRP is the column sum vector of estimated class reference matrix,  $\hat{\Pi}_c$ 

LCD Latent Class Distribution table.see also plot.exametrika

CMD Class Membership Distribution table. see also plot.exametrika

**Students** Class Membership Profile matrix. The s-th row vector of  $\hat{M}_c$ ,  $\hat{m}_c$ , is the class membership profile of Student s, namely the posterior probability distribution representing the student's belonging to the respective latent classes. The last column indicates the latent class estimate.

**IRP** Item Reference Profile matrix. The IRP of item j is the j-th row vector in the class reference matrix,  $\hat{\pi}_c$ 

ItemFitIndices Fit index for each item. See also ItemFit

**TestFitIndices** Overall fit index for the test. See also TestFit

```
# Fit a Latent Class Analysis model with 5 classes to the sample dataset
result.LCA <- LCA(J15S500, ncls = 5)

# Display the first few rows of student class membership probabilities
head(result.LCA$Students)

# Plot Item Response Profiles (IRP) for items 1-6 in a 2x3 grid
plot(result.LCA, type = "IRP", items = 1:6, nc = 2, nr = 3)

# Plot Class Membership Probabilities (CMP) for students 1-9 in a 3x3 grid
plot(result.LCA, type = "CMP", students = 1:9, nc = 3, nr = 3)

# Plot Test Response Profile (TRP) showing response patterns across all classes
plot(result.LCA, type = "TRP")

# Plot Latent Class Distribution (LCD) showing the size of each latent class
plot(result.LCA, type = "LCD")</pre>
```

40 LDB

LDB

Local Dependence Biclustering

# Description

Latent dependence Biclustering, which incorporates biclustering and a Bayesian network model.

# Usage

```
LDB(
U,
Z = NULL,
w = NULL,
na = NULL,
ncls = 2,
method = "R",
conf = NULL,
g_list = NULL,
adj_list = NULL,
adj_file = NULL,
verbose = FALSE
)
```

U	U is either a data class of exametrika, or raw data. When raw data is given, it is converted to the exametrika class with the dataFormat function.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
na	na argument specifies the numbers or characters to be treated as missing values.
ncls	number of latent class(rank). The default is 2.
method	specify the model to analyze the data. Local dependence latent class model is set to "C", latent rank model is set "R". The default is "R".
conf	For the confirmatory parameter, you can input either a vector with items and corresponding fields in sequence, or a field membership profile matrix. In the case of the former, the field membership profile matrix will be generated internally. When providing a membership profile matrix, it needs to be either matrix or data.frame. The number of fields(nfld) will be overwrite to the number of columns of this matrix.
g_list	A list compiling graph-type objects for each rank/class.
adj_list	A list compiling matrix-type adjacency matrices for each rank/class.
adj_file	A file detailing the relationships of the graph for each rank/class, listed in the order of starting point, ending point, and rank(class).
verbose	verbose output Flag. default is TRUE

LDB 41

#### Value

**nobs** Sample size. The number of rows in the dataset.

**testlength** Length of the test. The number of items included in the test.

**Nclass** Optimal number of classes.

Nfield Optimal number of fields.

crr Correct Response Rate

ItemLabel Label of Items

FieldLabel Label of Fields

adj\_list List of Adjacency matrix used in the model

**g\_list** List of graph object used in the model

**IRP** List of Estimated Parameters. This object is three-dimensional PIRP array, where each dimension represents the number of rank,number of field, and Dmax. Dmax denotes the maximum number of correct response patterns for each field.

**LFD** Latent Field Distribution. see also plot.exametrika

**LRD** Latent Rank Distribution. see also plot.exametrika

FRP Marginal Field Reference Matrix

**FRPIndex** Index of FFP includes the item location parameters B and Beta, the slope parameters A and Alpha, and the monotonicity indices C and Gamma.

**CCRR\_table** This table is a rearrangement of IRP into a data.frame format for output, consisting of combinations of rank ,field and PIRP.

TRP Test Reference Profile

**RMD** Rank Membership Distribution.

FieldEstimated Given vector which correspondence between items and the fields.

**ClassEstimated** An index indicating which class a student belongs to, estimated by confirmatory Ranklustering.

**Students** Rank Membership Profile matrix. The s-th row vector of  $\hat{M}_R$ ,  $\hat{m}_R$ , is the rank membership profile of Student s, namely the posterior probability distribution representing the student's belonging to the respective latent classes. It also includes the rank with the maximum estimated membership probability, as well as the rank-up odds and rank-down odds.

TestFitIndices Overall fit index for the test. See also TestFit

```
# Example: Latent Dirichlet Bayesian Network model
# Create field configuration vector based on field assignments
conf <- c(
   1, 6, 6, 8, 9, 9, 4, 7, 7, 7, 5, 8, 9, 10, 10, 9, 9,
   10, 10, 10, 2, 2, 3, 3, 5, 5, 6, 9, 9, 10, 1, 1, 7, 9, 10
)
# Create edge data for the network structure between fields
edges_data <- data.frame(
   "From Field (Parent) >>>" = c(
```

42 LDB

```
6, 4, 5, 1, 1, 4, # Class/Rank 2
    3, 4, 6, 2, 4, 4, # Class/Rank 3
   3, 6, 4, 1, # Class/Rank 4
   7, 9, 6, 7 # Class/Rank 5
  ">>> To Field (Child)" = c(
   8, 7, 8, 7, 2, 5, # Class/Rank 2
    5, 8, 8, 4, 6, 7, # Class/Rank 3
   5, 8, 5, 8, # Class/Rank 4
   10, 10, 8, 9 # Class/Rank 5
  ),
  "At Class/Rank (Locus)" = c(
    2, 2, 2, 2, 2, # Class/Rank 2
   3, 3, 3, 3, 3, # Class/Rank 3
   4, 4, 4, # Class/Rank 4
   5, 5, 5, 5 # Class/Rank 5
  )
)
# Save edge data to temporary CSV file
tmp_file <- tempfile(fileext = ".csv")</pre>
write.csv(edges_data, file = tmp_file, row.names = FALSE)
# Fit Latent Dirichlet Bayesian Network model
result.LDB <- LDB(</pre>
  U = J35S515,
  ncls = 5, # Number of latent classes
  conf = conf, # Field configuration vector
  adj_file = tmp_file # Path to the CSV file
)
# Clean up temporary file
unlink(tmp_file)
# Display model results
print(result.LDB)
# Visualize different aspects of the model
plot(result.LDB, type = "Array") # Show bicluster structure
plot(result.LDB, type = "TRP") # Test Response Profile
plot(result.LDB, type = "LRD") # Latent Rank Distribution
plot(result.LDB,
  type = "RMP", # Rank Membership Profiles
  students = 1:9, nc = 3, nr = 3
)
plot(result.LDB,
  type = "FRP", # Field Reference Profiles
  nc = 3, nr = 2
# Field PIRP Profile showing correct answer counts for each rank and field
plot(result.LDB, type = "FieldPIRP")
```

LDLRA 43

LDLRA

Local Dependence Latent Rank Analysis

# Description

performs local dependence latent lank analysis(LD\_LRA) by Shojima(2011)

# Usage

```
LDLRA(
U,
Z = NULL,
w = NULL,
na = NULL,
ncls = 2,
method = "R",
g_list = NULL,
adj_list = NULL,
adj_file = NULL,
verbose = FALSE
)
```

# Arguments

U	U is either a data class of exametrika, or raw data. When raw data is given, it is converted to the exametrika class with the dataFormat function.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
na	na argument specifies the numbers or characters to be treated as missing values.
ncls	number of latent class(rank). The default is 2.
method	specify the model to analyze the data. Local dependence latent class model is set to "C", latent rank model is set "R". The default is "R".
g_list	A list compiling graph-type objects for each rank/class.
adj_list	A list compiling matrix-type adjacency matrices for each rank/class.
adj_file	A file detailing the relationships of the graph for each rank/class, listed in the order of starting point, ending point, and rank(class).
verbose	verbose output Flag. default is TRUE

# **Details**

This function is intended to perform LD-LRA. LD-LRA is an analysis that combines LRA and BNM, and it is used to analyze the network structure among items in the latent rank. In this function, structural learning is not performed, so you need to provide item graphs for each rank as separate files. The file format for this is plain text CSV that includes edges (From, To) and rank numbers.

44 LDLRA

#### Value

**nobs** Sample size. The number of rows in the dataset.

testlength Length of the test. The number of items included in the test.

crr correct response ratio

adj\_list adjacency matrix list

g\_list graph list

**referenceMatrix** Learned Parameters.A three-dimensional array of patterns where item x rank x pattern.

**IRP** Marginal Item Reference Matrix

IRPIndex IRP Indices which include Alpha, Beta, Gamma.

TRP Test Reference Profile matrix.

LRD latent Rank/Class Distribution

RMD Rank/Class Membership Distribution

TestFitIndices Overall fit index for the test. See also TestFit

Estimation\_table Estimated parameters tables.

**CCRR\_table** Correct Response Rate tables

**Studens** Student information. It includes estimated class membership, probability of class membership, RUO, and RDO.

```
# Create sample DAG structure with different rank levels
# Format: From, To, Rank
DAG_dat <- matrix(c(</pre>
  "From", "To", "Rank"
  "Item01", "Item02", "1", # Simple structure for Rank 1
  "Item01", "Item02", "2", # More complex structure for Rank 2
  "Item02", "Item03", "2"
  "Item01", "Item02", "3", # Additional connections for Rank 3
  "Item02", "Item03", "3"
  "Item03", "Item04", "3"
), ncol = 3, byrow = TRUE)
# Method 1: Directly use graph and adjacency lists
g_list <- list()</pre>
adj_list <- list()
for (i in 1:3) {
  adj_R <- DAG_dat[DAG_dat[, 3] == as.character(i), 1:2, drop = FALSE]</pre>
  g_tmp <- igraph::graph_from_data_frame(</pre>
    d = data.frame(
     From = adj_R[, 1],
      To = adj_R[, 2]
    ),
    directed = TRUE
```

LD\_param\_est 45

```
adj_tmp <- igraph::as_adjacency_matrix(g_tmp)</pre>
  g_list[[i]] \leftarrow g_tmp
  adj_list[[i]] <- adj_tmp</pre>
}
# Fit Local Dependence Latent Rank Analysis
result.LDLRA1 <- LDLRA(J12S5000,
  ncls = 3,
  g_list = g_list,
  adj_list = adj_list
)
# Plot Item Reference Profiles (IRP) in a 4x3 grid
# Shows the probability patterns of correct responses for each item across ranks
plot(result.LDLRA1, type = "IRP", nc = 4, nr = 3)
# Plot Test Reference Profile (TRP)
# Displays the overall pattern of correct response probabilities across ranks
plot(result.LDLRA1, type = "TRP")
# Plot Latent Rank Distribution (LRD)
# Shows the distribution of students across different ranks
plot(result.LDLRA1, type = "LRD")
```

LD\_param\_est

LDparam set

#### **Description**

A function that extracts only the estimation of graph parameters after the rank estimation is completed.

#### Usage

```
LD_param_est(tmp, adj_list, classRefMat, ncls, smoothpost)
```

# **Arguments**

```
tmp
adj_list
classRefMat
values returned from emclus
```

ncls ncls

smoothpost smoothpost

46 LRA

LogisticModel

Four-Parameter Logistic Model

# **Description**

The four-parameter logistic model is a model where one additional parameter d, called the upper asymptote parameter, is added to the 3PLM.

# Usage

```
LogisticModel(a = 1, b, c = 0, d = 1, theta)
```

# **Arguments**

a	slope parameter
b	location parameter
С	lower asymptote parameter
d	upper asymptote parameter
theta	ability parameter

# Value

Returns a numeric vector of probabilities between c and d, representing the probability of a correct response given the ability level theta. The probability is calculated using the formula:  $P(\theta) = c + \frac{(d-c)}{1+e^{-a(\theta-b)}}$ 

LRA

Latent Rank Analysis

# **Description**

A function for estimating LRA by SOM/GTM

# Usage

```
LRA(
   U,
   nrank = 2,
   na = NULL,
   Z = NULL,
   w = NULL,
   method = "GTM",
   mic = FALSE,
   maxiter = 100,
   BIC.check = FALSE,
   seed = NULL
)
```

LRA 47

#### **Arguments**

U is either a data class of exametrika, or raw data. When raw data is given, it is

converted to the exametrika class with the dataFormat function.

nrank number of latent rank

na argument specifies the numbers or characters to be treated as missing values.

Z is a missing indicator matrix of the type matrix or data.frame

w w is item weight vector

method Specify either "SOM" or "GTM". SOM refers to the estimation method using

Self-Organizing Mapping, which is suitable when the data size is small. However, as the sample size increases, it takes time to execute. GTM is a batch learning type of SOM, equivalent to applying a gentle filter to LCA (Shojima,

2022).

mic Monotonic increasing IRP option. The default is FALSE.

maxiter Maximum number of iterations. default is 100.

BIC.check During estimation with SOM, this parameter determines whether to use the

change in BIC as the convergence criterion. By default, it is FALSE and iteration continues until the maximum number of iterations is reached. If set to TRUE, iteration continues until the overall change in BIC falls below a negligible amount, or until the iteration count reaches ten times the maximum number

of iterations.

seed random seed for SOM. If not specified, a value derived from the original data

will be automatically assigned.

#### Value

**nobs** Sample size. The number of rows in the dataset.

testlength Length of the test. The number of items included in the test.

Nclass number of classes you set

**TRP** Test Reference Profile matrix. The TRP is the column sum vector of estimated class reference matrix,  $\hat{\Pi}_c$ 

LCD Latent Class Distribution table.see also plot.exametrika

**CMD** Class Membership Distribution table. see also plot.exametrika

**Students** Class Membership Profile matrix. The s-th row vector of  $\hat{M}_c$ ,  $\hat{m}_c$ , is the class membership profile of Student s, namely the posterior probability distribution representing the student's belonging to the respective latent classes. It also includes the rank with the maximum estimated membership probability, as well as the rank-up odds and rank-down odds.

IRP Item Reference Profile matrix. The IRP of item j is the j-th row vector in the class reference matrix,  $\hat{\pi}_c$ 

**IRPIndex** The IRP information includes the item location parameters B and Beta, the slope parameters A and Alpha, and the monotonicity indices C and Gamma.

ItemFitIndices Fit index for each item. See also ItemFit

TestFitIndices Overall fit index for the test. See also TestFit

48 maxParents\_penalty

#### **Examples**

```
# Fit a Latent Rank Analysis model with 6 ranks to the sample dataset
result.LRA <- LRA(J15S500, nrank = 6)
# Display the first few rows of student rank membership profiles
# This shows posterior probabilities of students belonging to each rank
head(result.LRA$Students)
# Plot Item Reference Profiles (IRP) for items 1-6 in a 2x3 grid
# Shows the probability of correct response for each rank
plot(result.LRA, type = "IRP", items = 1:6, nc = 2, nr = 3)
# Plot Rank Membership Profiles (RMP) for students 1-9 in a 3x3 grid
# Shows the posterior probability distribution of rank membership for each student
plot(result.LRA, type = "RMP", students = 1:9, nc = 3, nr = 3)
# Plot Test Reference Profile (TRP)
# Shows the column sum vector of estimated rank reference matrix
plot(result.LRA, type = "TRP")
# Plot Latent Rank Distribution (LRD)
# Shows the distribution of students across different ranks
plot(result.LRA, type = "LRD")
```

maxParents\_penalty

Utility function for searching DAG

# Description

Function to limit the number of parent nodes

# Usage

```
maxParents_penalty(vec, testlength, maxParents)
```

#### **Arguments**

vec gene Vector corresponding to the upper triangular of the adjacency matrix

test length test length. In this context it means a number of nodes.

maxParents Upper limit of number of nodes.

## **Details**

When generating an adjacency matrix using GA, the number of edges coming from a single node should be limited to 2 or 3. This is because if there are too many edges, it becomes difficult to interpret in practical applications. This function works to adjust the sampling of the randomly

MutualInformation 49

generated adjacency matrix so that the column sum of the upper triangular elements fits within the set limit.

MutualInformation

Mutual Information

# Description

Mutual Information is a measure that represents the degree of interdependence between two items. This function is applicable only to binary response data. The measure is calculated using the joint probability distribution of responses between item pairs and their marginal probabilities.

# Usage

```
MutualInformation(U, na = NULL, Z = NULL, w = NULL, ...)
```

# **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
• • •	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

# Value

A matrix of mutual information values with exametrika class. Each element (i,j) represents the mutual information between items i and j, measured in bits. Higher values indicate stronger interdependence between items.

## Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

```
# example code
# Calculate Mutual Information using sample dataset J15S500
MutualInformation(J15S500)
```

50 nrs

nrs

Number Right Score

## **Description**

The Number-Right Score (NRS) function calculates the weighted sum of correct responses for each examinee. This function is applicable only to binary response data.

For each examinee, the score is computed as:

$$NRS_i = \sum_{j=1}^{J} z_{ij} u_{ij} w_j$$

where:

- $z_{ij}$  is the missing response indicator (0/1)
- $u_{ij}$  is the response (0/1)
- $w_i$  is the item weight

# Usage

```
nrs(U, na = NULL, Z = NULL, w = NULL, ...)
```

# **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
•••	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

# Value

A numeric vector containing the Number-Right Score for each examinee. The score represents the weighted sum of correct answers, where:

- Maximum score is the sum of all item weights
- Minimum score is 0
- Missing responses do not contribute to the score

# Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

#### **Examples**

```
# using sample dataset
nrs(J15S500)
```

```
objective_function_IRT
```

Log-likelihood function used in the Maximization Step (M-Step).

# Description

Log-likelihood function used in the Maximization Step (M-Step).

# Usage

```
objective_function_IRT(lambda, model, qjtrue, qjfalse, quadrature)
```

# **Arguments**

lambda item parameter vector

model 2,3,or 4 PL

qjtrue correct resp pattern qjfalse incorrect resp pattern

quadrature Pattern of a segmented normal distribution.

OmegaCoefficient Omega Coefficient

# Description

This function computes Tau-Congeneric Measurement, also known as McDonald's tau coefficient, for a given data set.

# Usage

```
OmegaCoefficient(x, na = NULL, Z = NULL, w = NULL)
```

# **Arguments**

X	This should be a data matrix or a Covariance/Phi/Tetrachoric matrix.
na	This parameter identifies the numbers or characters that should be treated as missing values when 'x' is a data matrix.
Z	This parameter represents a missing indicator matrix. It is only needed if 'x' is a data matrix.

w This parameter is an item weight vector. It is only required if 'x' is a data matrix.

52 passage

#### Value

For a correlation/covariance matrix input, returns a single numeric value representing the omega coefficient. For a data matrix input, returns a list with three components:

- OmegaCov: Omega coefficient calculated from covariance matrix
- OmegaPhi: Omega coefficient calculated from phi coefficient matrix
- OmegaTetrachoric: Omega coefficient calculated from tetrachoric correlation matrix

#### References

McDonald, R. P. (1999). Test theory: A unified treatment. Erlbaum.

passage

Passage Rate of Student

# **Description**

The Passage Rate for each student is calculated as their Number-Right Score (NRS) divided by the number of items presented to them. This function is applicable only to binary response data.

The passage rate is calculated as:

$$P_{i} = \frac{\sum_{j=1}^{J} z_{ij} u_{ij} w_{j}}{\sum_{j=1}^{J} z_{ij}}$$

where:

- $z_{ij}$  is the missing response indicator (0/1)
- $u_{ij}$  is the response (0/1)
- $w_j$  is the item weight

# Usage

```
passage(U, na = NULL, Z = NULL, w = NULL, ...)
```

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
•••	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

percentile 53

#### Value

A numeric vector containing the passage rate for each student. Values range from 0 to 1 (or maximum weight) where:

- 1: Perfect score on all attempted items
- 0: No correct answers
- NA: No items attempted

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

The passage rate accounts for missing responses by only considering items that were actually presented to each student. This provides a fair comparison between students who attempted different numbers of items.

#### **Examples**

```
# using sample dataset
passage(J15S500)
```

percentile

Student Percentile Ranks

# **Description**

The percentile function calculates each student's relative standing in the group, expressed as a percentile rank (1-100). This function is applicable only to binary response data.

The percentile rank indicates the percentage of scores in the distribution that fall below a given score. For example, a percentile rank of 75 means the student performed better than 75% of the group.

# Usage

```
percentile(U, na = NULL, Z = NULL, w = NULL, ...)
```

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

PhiCoefficient

#### Value

A numeric vector of percentile ranks (1-100) for each student, where:

- 100: Highest performing student(s)
- 50: Median performance
- 1: Lowest performing student(s)

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

Percentile ranks are calculated using the empirical cumulative distribution function of standardized scores. Tied scores receive the same percentile rank. The values are rounded up to the nearest integer to provide ranks from 1 to 100.

# **Examples**

```
# using sample dataset
percentile(J5S10)
```

PhiCoefficient

Phi-Coefficient

# Description

The phi coefficient is the Pearson's product moment correlation coefficient between two binary items. This function is applicable only to binary response data. The coefficient ranges from -1 to 1, where 1 indicates perfect positive correlation, -1 indicates perfect negative correlation, and 0 indicates no correlation.

# Usage

```
PhiCoefficient(U, na = NULL, Z = NULL, w = NULL, ...)
```

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

plot.exametrika 55

#### Value

A matrix of phi coefficients with exametrika class. Each element (i,j) represents the phi coefficient between items i and j. The matrix is symmetric with ones on the diagonal.

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

## **Examples**

```
# example code
# Calculate Phi-Coefficient using sample dataset J15S500
PhiCoefficient(J15S500)
```

plot.exametrika

Plotting functions for the exametrika package of class "exametrika"

## Description

The calculation results of the exametrika package have an exametrika class attribute. In addition, the class name of the analysis model is also assigned. The models are listed as follows: IRT, LCA, LRA, Biclustering, IRM, LDLRA, LDB, BINET. A plot is made for each model. Although the analysis results are visualized from various perspectives, they correspond by specifying the 'type' variable when plotting.

#### Usage

```
## S3 method for class 'exametrika'
plot(
    x,
    type = c("IIC", "ICC", "TIC", "IRP", "TRP", "LCD", "CMP", "FRP", "RMP", "LRD", "Array",
        "FieldPIRP", "LDPSR"),
    items = NULL,
    students = NULL,
    nc = 1,
    nr = 1,
    ...
)
```

```
    x exametrika Class object
    type
    Plot type.The selectable type names are as follows: IIC, ICC, TIC, IRP, TRP, LCD, CMP, FRP, RMP, LRD, Array, FieldPRIP, LDPSR.
    ICC Item Characteristic Curve. For IRT model
```

56 plot.exametrika

**IIC** Item Information Curve. For IRT model. When specifying the item numbers with the items option, giving 0 will make it TIC.

- TIC Test Information Curve. For IRT model
- **IRP** Item Reference Profile.IRP is a line graph with items and latent classes/ranks on the horizontal axis, and membership probability on the vertical axis. This type can be selected when using LCA,LRA,Biclustering and LDB model.
- **TRP** Test Reference Profile. TRP is a representation that uses the latent classes/ranks on the horizontal axis. It simultaneously displays the number of members belonging to each class/rank) as a bar graph and the expected test scores as a line graph. This type can be selected for all models except IRT.
- **LCD** Latent Class Distribution. LCD is a graph that takes latent classes on the horizontal axis, represents the number of members belonging to each class with a bar graph, and plots the cumulative predicted membership probability with a line graph. It can be selected for all models except IRT.
- **LRD** Latent Rank Distribution. The difference between LRD and LCD is whether the horizontal axis represents classes or ranks.
- **CMP** Class Membership Profile.CMP is a line graph representing the class membership probabilities of students. Since one graph is drawn for each student, using the 'students' option allows you to specify which students to display. Additionally, with the 'nr' and 'nc' options, you should ensure the ability to display multiple figures.
- **RMP** Rank Membership Profile. The difference between RMP and CMP is whether the horizontal axis represents classes or ranks.
- **FRP** Field Reference Profile. "FRP is a diagram depicting the correspondence between the field and the latent class/rank. It represents the expected correct answer rate of members belonging to a particular latent class/rank using a line graph.
- **Array** Array plot for Biclustering/Ranklustering. An Array plot is a diagram coloring the matrix cells, in which the larger the cell value, the darker the cell color. In this plot of the binary raw data, the corrected responses are shaded in black, and the black-and-white pattern appears to be random. However, after being classified by biclustering, students' answer patterns and items' answer patterns are each sorted based on similarity. Thus, the divisions made by the clustering are visually evident.
- **FieldPIRP** This type can only be selected in the LDB model. The horizontal axis represents the number of correct answers in the parent field, while the vertical axis represents the correct response rate in the specified rank. A line graph is drawn for each item included in the field.
- **LDPSR** Latent Dependence Passing Student Rate shows that is a graph that takes items in field j on the horizontal axis and represents the passing rates of both parent and child classes on the graph.

Specify the items you want to plot as a vector. If not specifically designated, all items will be included. When the type is IIC, if the specified item is 0, it returns a TIC representing the entire test.

Specify the numbers of the students you want to plot as a vector. If not specifically designated, all students will be included.

items

students

print.exametrika 57

nc	Specifying the number of columns when there are many plots to be drawn. The default is 1.
nr	Specifying the number of rows when there are many plots to be drawn. The default is 1.
	other options

#### **Details**

- "IRT": Can only have types "ICC", "IIC", "TIC".
- "LCA": Can only have types "IRP", "FRP", "TRP", "LCD", "CMP".
- "LRA": Can only have types "IRP", "FRP", "TRP", "LRD", "RMP".
- "Biclustering": Can only have types "IRP", "FRP", "LCD", "LRD", "CMP", "RMP", "Array".
- "IRM": Can only have types "FRP", "TRP", "Array".
- "LDLRA": Can only have types "IRP", "TRP", "LRD", "RMP".
- "LDB": Can only have types "FRP", "TRP", "LRD", "RMP", "Array", "FieldPIRP".
- "BINET": Can only have types "FRP", "TRP", "LRD", "RMP", "Array", "LDPSR".

#### Value

Produces different types of plots depending on the class of the input object and the specified type:

- For IRT models: ICC (Item Characteristic Curves), IIC (Item Information Curves), or TIC (Test Information Curves)
- For LCA/LRA models: IRP (Item Reference Profile), TRP (Test Reference Profile), LCD/LRD (Latent Class/Rank Distribution), CMP/RMP (Class/Rank Membership Profile)
- For Biclustering/IRM models: Array plots showing clustering patterns
- For LDLRA/LDB/BINET models: Various network and profile plots specific to each model

The function returns NULL invisibly.

```
print.exametrika print.exametrika
```

#### **Description**

Output format for exametrika Class

## Usage

```
## S3 method for class 'exametrika'
print(x, digits = 3, ...)
```

58 PSD\_item\_params

## **Arguments**

x exametrika Class object

digits printed digits
... other options

#### Value

Prints a formatted summary of the exametrika object to the console, with content varying by object class:

• TestStatistics: Basic descriptive statistics of the test

• Dimensionality: Eigenvalue analysis results with scree plot

• ItemStatistics: Item-level statistics

• CTT: Classical Test Theory reliability measures

• IRT: Item parameters and fit indices

• LCA/LRA: Class/Rank profiles and model fit information

• Biclustering/IRM: Cluster profiles and model diagnostics

• Network models (LDLRA/LDB/BINET): Network visualizations and parameter estimates

PSD\_item\_params

internal functions for PSD of Item parameters

## **Description**

internal functions for PSD of Item parameters

#### Usage

```
PSD_item_params(model, Lambda, quadrature, marginal_posttheta)
```

#### **Arguments**

model 2,3,or 4PL

Lambda item parameters Matrix

quadrature quads
marginal\_posttheta

marginal post theta

RaschModel 59

|--|

# Description

The one-parameter logistic model is a model with only one parameter b. This model is a 2PLM model in which a is constrained to 1. This model is also called the Rasch model.

## Usage

```
RaschModel(b, theta)
```

# **Arguments**

b slope parameter theta ability parameter

# Value

Returns a numeric vector of probabilities between 0 and 1, representing the probability of a correct response given the ability level theta. The probability is calculated using the formula:  $P(\theta) = \frac{1}{1+e^{-(\theta-b)}}$ 

slopeprior
------------

Prior distribution function with respect to the slope.

# Description

Prior distribution function with respect to the slope.

## Usage

```
slopeprior(a, m, s, const = 1e-15)
```

# Arguments

a	slope coefficient
---	-------------------

m prior parameter to be set
s prior parameter to be set
const A very small constant

sscore sscore

softmax

softmax function

# Description

to avoid overflow

# Usage

softmax(x)

# **Arguments**

Χ

numericvector

sscore

Standardized Score

# Description

The standardized score (z-score) indicates how far a student's performance deviates from the mean in units of standard deviation. This function is applicable only to binary response data.

The score is calculated by standardizing the passage rates:

$$Z_i = \frac{r_i - \bar{r}}{\sigma_r}$$

where:

- $r_i$  is student i's passage rate
- $\bar{r}$  is the mean passage rate
- $\sigma_r$  is the standard deviation of passage rates

# Usage

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
•••	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

stanine 61

#### Value

A numeric vector of standardized scores for each student. The scores follow a standard normal distribution with:

- Mean = 0
- Standard deviation = 1
- Approximately 68% of scores between -1 and 1
- Approximately 95% of scores between -2 and 2
- Approximately 99% of scores between -3 and 3

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

The standardization allows for comparing student performance across different tests or groups. A positive score indicates above-average performance, while a negative score indicates below-average performance.

# **Examples**

```
# using sample dataset
sscore(J5S10)
```

stanine

Stanine Scores

# **Description**

The Stanine (Standard Nine) scoring system divides students into nine groups based on a normalized distribution. This function is applicable only to binary response data.

These groups correspond to the following percentile ranges:

- Stanine 1: lowest 4% (percentiles 1-4)
- Stanine 2: next 7% (percentiles 5-11)
- Stanine 3: next 12% (percentiles 12-23)
- Stanine 4: next 17% (percentiles 24-40)
- Stanine 5: middle 20% (percentiles 41-60)
- Stanine 6: next 17% (percentiles 61-77)
- Stanine 7: next 12% (percentiles 78-89)
- Stanine 8: next 7% (percentiles 90-96)
- Stanine 9: highest 4% (percentiles 97-100)

62 stanine

## Usage

```
stanine(U, na = NULL, Z = NULL, w = NULL, ...)
```

# Arguments

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
•••	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

#### Value

A list containing two elements:

```
stanine The score boundaries for each stanine level stanineScore The stanine score (1-9) for each student
```

#### Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

Stanine scores provide a normalized scale with:

- Mean = 5
- Standard deviation = 2
- Scores range from 1 to 9
- Score of 5 represents average performance

#### References

Angoff, W. H. (1984). Scales, norms, and equivalent scores. Educational Testing Service. (Reprint of chapter in R. L. Thorndike (Ed.) (1971) Educational Measurement (2nd Ed.). American Council on Education.

```
result <- stanine(J15S500)
# View score boundaries
result$stanine
# View individual scores
result$stanineScore</pre>
```

StrLearningGA\_BNM

Structure Learning for BNM by simple GA

# Description

Generating a DAG from data using a genetic algorithm.

# Usage

```
StrLearningGA_BNM(
 U,
 Z = NULL
 w = NULL,
  na = NULL,
  seed = 123,
  population = 20,
 Rs = 0.5,
 Rm = 0.005,
 maxParents = 2,
 maxGeneration = 100,
  successiveLimit = 5,
  crossover = 0,
  elitism = 0,
  filename = NULL,
  verbose = TRUE
)
```

# **Arguments**

successiveLimit

U	U is either a data class of exametrika, or raw data. When raw data is given, it is converted to the exametrika class with the dataFormat function.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
na	na argument specifies the numbers or characters to be treated as missing values.
seed	seed for random.
population	Population size. The default is 20
Rs	Survival Rate. The default is 0.5
Rm	Mutation Rate. The default is 0.005
maxParents	Maximum number of edges emanating from a single node. The default is 2.
maxGeneration	Maximum number of generations.

Termination conditions. If the optimal individual does not change for this number of generations, it is considered to have converged.

crossover	Configure crossover using numerical values. Specify 0 for uniform crossover, where bits are randomly copied from both parents. Choose 1 for single-point crossover with one crossover point, and 2 for two-point crossover with two crossover points. The default is 0.
elitism	Number of elites that remain without crossover when transitioning to the next generation.
filename	Specify the filename when saving the generated adjacency matrix in CSV format. The default is null, and no output is written to the file.
verbose	verbose output Flag. default is TRUE

#### **Details**

This function generates a DAG from data using a genetic algorithm. Depending on the size of the data and the settings, the computation may take a significant amount of computational time. For details on the settings or algorithm, see Shojima(2022), section 8.5

#### Value

```
adj Optimal adjacency matrix
testlength Length of the test. The number of items included in the test.
TestFitIndices Overall fit index for the test. See also TestFit
nobs Sample size. The number of rows in the dataset.
testlength Length of the test. The number of items included in the test.
crr correct response ratio
TestFitIndices Overall fit index for the test. See also TestFit
adj Adjacency matrix
param Learned Parameters
CCRR_table Correct Response Rate tables
```

```
# Perform Structure Learning for Bayesian Network Model using Genetic Algorithm
# Parameters are set for balanced exploration and computational efficiency
StrLearningGA_BNM(J5S10,
   population = 20, # Size of population in each generation
   Rs = 0.5, # 50% survival rate for next generation
   Rm = 0.002, # 0.2% mutation rate for genetic diversity
   maxParents = 2, # Maximum of 2 parent nodes per item
   maxGeneration = 100, # Maximum number of evolutionary steps
   crossover = 2, # Use two-point crossover method
   elitism = 2 # Keep 2 best solutions in each generation
)
```

StrLearningPBIL\_BNM Structure Learning for BNM by PBIL

# **Description**

Generating a DAG from data using a Population-Based Incremental Learning

# Usage

```
StrLearningPBIL_BNM(
 U,
 Z = NULL
 w = NULL,
 na = NULL,
  seed = 123,
 population = 20,
 Rs = 0.5,
 Rm = 0.002,
 maxParents = 2,
 maxGeneration = 100,
 successiveLimit = 5,
  elitism = 0,
  alpha = 0.05,
 estimate = 1,
  filename = NULL,
  verbose = TRUE
)
```

# Arguments

U	U is either a data class of exametrika, or raw data. When raw data is given, it is converted to the exametrika class with the dataFormat function.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
na	na argument specifies the numbers or characters to be treated as missing values.
seed	seed for random.
population	Population size. The default is 20
Rs	Survival Rate. The default is 0.5
Rm	Mutation Rate. The default is 0.002
maxParents	Maximum number of edges emanating from a single node. The default is 2.
${\it maxGeneration}$	Maximum number of generations.
successiveLimit	

Termination conditions. If the optimal individual does not change for this number of generations, it is considered to have converged.

elitism Number of elites that remain without crossover when transitioning to the next

generation.

alpha Learning rate. The default is 0.05

estimate In PBIL for estimating the adjacency matrix, specify by number from the fol-

lowing four methods: 1. Optimal adjacency matrix, 2. Rounded average of individuals in the last generation, 3. Rounded average of survivors in the last generation, 4. Rounded generational gene of the last generation. The default is

1.

filename Specify the filename when saving the generated adjacency matrix in CSV for-

mat. The default is null, and no output is written to the file.

verbose verbose output Flag. default is TRUE

# **Details**

This function performs structural learning using the Population-Based Incremental Learning model(PBIL) proposed by Fukuda et al.(2014) within the genetic algorithm framework. Instead of learning the adjacency matrix itself, the 'genes of genes' that generate the adjacency matrix are updated with each generation. For more details, please refer to Fukuda(2014) and Section 8.5.2 of the text(Shojima,2022).

#### Value

adj Optimal adjacency matrix

testlength Length of the test. The number of items included in the test.

TestFitIndices Overall fit index for the test. See also TestFit

**nobs** Sample size. The number of rows in the dataset.

testlength Length of the test. The number of items included in the test.

crr correct response ratio

**TestFitIndices** Overall fit index for the test. See also TestFit

param Learned Parameters

**CCRR** table Correct Response Rate tables

## References

Fukuda, S., Yamanaka, Y., & Yoshihiro, T. (2014). A Probability-based evolutionary algorithm with mutations to learn Bayesian networks. International Journal of Artificial Intelligence and Interactive Multimedia, 3, 7–13. DOI: 10.9781/ijimai.2014.311

```
# Perform Structure Learning for Bayesian Network Model using PBIL
# (Population-Based Incremental Learning)
StrLearningPBIL_BNM(J5S10,
   population = 20, # Size of population in each generation
   Rs = 0.5, # 50% survival rate for next generation
   Rm = 0.005, # 0.5% mutation rate for genetic diversity
```

```
maxParents = 2, # Maximum of 2 parent nodes per item
alpha = 0.05, # Learning rate for probability update
estimate = 4 # Use rounded generational gene method
)
```

StrLearningPBIL\_LDLRA Structure Learning for LDLRA by PBIL algorithm

# **Description**

Generating DAG list from data using Population-Based Incremental learning

# Usage

```
StrLearningPBIL_LDLRA(
 U,
 Z = NULL,
 w = NULL,
 na = NULL,
  seed = 123,
 ncls = 2,
 method = "R",
 population = 20,
 Rs = 0.5,
 Rm = 0.002,
 maxParents = 2,
 maxGeneration = 100,
  successiveLimit = 5,
 elitism = 0,
 alpha = 0.05,
 estimate = 1,
  filename = NULL,
  verbose = TRUE
)
```

U	U is either a data class of exametrika, or raw data. When raw data is given, it is converted to the exametrika class with the dataFormat function.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
na	na argument specifies the numbers or characters to be treated as missing values.
seed	seed for random.
ncls	number of latent class(rank). The default is 2.

method specify the model to analyze the data. Local dependence latent class model is set

to "C", latent rank model is set "R". The default is "R".

population Population size. The default is 20
Rs Survival Rate. The default is 0.5
Rm Mutation Rate. The default is 0.002

maxParents Maximum number of edges emanating from a single node. The default is 2.

maxGeneration Maximum number of generations.

successiveLimit

Termination conditions. If the optimal individual does not change for this num-

ber of generations, it is considered to have converged.

elitism Number of elites that remain without crossover when transitioning to the next

generation.

alpha Learning rate. The default is 0.05

estimate In PBIL for estimating the adjacency matrix, specify by number from the fol-

lowing four methods: 1. Optimal adjacency matrix, 2. Rounded average of individuals in the last generation, 3. Rounded average of survivors in the last generation, 4. Rounded generational gene of the last generation. The default is

1.

filename Specify the filename when saving the generated adjacency matrix in CSV for-

mat. The default is null, and no output is written to the file.

verbose verbose output Flag. default is TRUE

#### **Details**

This function performs structural learning for each classes by using the Population-Based Incremental Learning model(PBIL) proposed by Fukuda et al.(2014) within the genetic algorithm framework. Instead of learning the adjacency matrix itself, the 'genes of genes' that generate the adjacency matrix are updated with each generation. For more details, please refer to Fukuda(2014) and Section 9.4.3 of the text(Shojima,2022).

# Value

**nobs** Sample size. The number of rows in the dataset.

testlength Length of the test. The number of items included in the test.

crr correct response ratio

adj\_list adjacency matrix list

**g\_list** graph list

**referenceMatrix** Learned Parameters.A three-dimensional array of patterns where item x rank x pattern.

**IRP** Marginal Item Reference Matrix

IRPIndex IRP Indices which include Alpha, Beta, Gamma.

TRP Test Reference Profile matrix.

LRD latent Rank/Class Distribution

StudentAnalysis 69

**RMD** Rank/Class Membership Distribution

TestFitIndices Overall fit index for the test. See also TestFit

Estimation\_table Estimated parameters tables.

**CCRR\_table** Correct Response Rate tables

**Studens** Student information. It includes estimated class membership, probability of class membership, RUO, and RDO.

#### References

Fukuda, S., Yamanaka, Y., & Yoshihiro, T. (2014). A Probability-based evolutionary algorithm with mutations to learn Bayesian networks. International Journal of Artificial Intelligence and Interactive Multimedia, 3, 7–13. DOI: 10.9781/ijimai.2014.311

# **Examples**

```
\# Perform Structure Learning for LDLRA using PBIL algorithm
# This process may take considerable time due to evolutionary optimization
result.LDLRA.PBIL <- StrLearningPBIL_LDLRA(J35S515,
 seed = 123, # Set random seed for reproducibility
 ncls = 5, # Number of latent ranks
 method = "R", # Use rank model (vs. class model)
 elitism = 1, # Keep best solution in each generation
 successiveLimit = 15 # Convergence criterion
)
# Examine the learned network structure
# Plot Item Response Profiles showing item patterns across ranks
plot(result.LDLRA.PBIL, type = "IRP", nc = 4, nr = 3)
# Plot Test Response Profile showing overall response patterns
plot(result.LDLRA.PBIL, type = "TRP")
# Plot Latent Rank Distribution showing student distribution
plot(result.LDLRA.PBIL, type = "LRD")
```

StudentAnalysis

StudentAnalysis

# Description

The StudentAnalysis function returns descriptive statistics for each individual student. Specifically, it provides the number of responses, the number of correct answers, the passage rate, the standardized score, the percentile, and the stanine.

## Usage

```
StudentAnalysis(U, na = NULL, Z = NULL, w = NULL)
```

70 TestFit

# **Arguments**

U is a data matrix of the type matrix or data.frame.

na argument specifies the numbers or characters to be treated as missing values.

• ID: Student identifier

• NR: Number of responses

• NRS: Number-right score (total correct answers)

• PR: Passage rate (proportion correct)

• SS: Standardized score (z-score)

• Percentile: Student's percentile rank

• Stanine: Student's stanine score (1-9)

Z is a missing indicator matrix of the type matrix or data.frame

w is item weight vector

# Value

Returns a data frame containing the following columns for each student:

• ID: Student identifier

• NR: Number of responses

• NRS: Number-right score (total correct answers)

• PR: Passage rate (proportion correct)

• SS: Standardized score (z-score)

• Percentile: Student's percentile rank

• Stanine: Student's stanine score (1-9)

# **Examples**

```
# using sample dataset
StudentAnalysis(J15S500)
```

TestFit

Model Fit Functions for test whole

## **Description**

A general function that returns the model fit indices.

# Usage

```
TestFit(U, Z, ell_A, nparam)
```

TestFitSaturated 71

#### **Arguments**

U is either a data class of exametrika, or raw data. When raw data is given, it is

converted to the exametrika class with the dataFormat function.

Z is a missing indicator matrix of the type matrix or data.frame

ell\_A log likelihood of this model

nparam number of parameters for this model

#### Value

model\_log\_like log likelihood of analysis model

bench\_log\_like log likelihood of benchmark model

null\_log\_like log likelihood of null model

model\_Chi\_sq Chi-Square statistics for analysis model

null\_Chi\_sq Chi-Square statistics for null model

model\_df degrees of freedom of analysis model

null\_df degrees of freedom of null model

NFI Normed Fit Index. Lager values closer to 1.0 indicate a better fit.

RFI Relative Fit Index. Lager values closer to 1.0 indicate a better fit.

**IFI** Incremental Fit Index. Lager values closer to 1.0 indicate a better fit.

TLI Tucker-Lewis Index. Lager values closer to 1.0 indicate a better fit.

CFI Comparative Fit Index. Lager values closer to 1.0 indicate a better fit.

RMSEA Root Mean Square Error of Approximation. Smaller values closer to 0.0 indicate a better fit

**AIC** Akaike Information Criterion. A lower value indicates a better fit.

CAIC Consistent AIC.A lower value indicates a better fit.

BIC Bayesian Information Criterion. A lower value indicates a better fit.

TestFitSaturated Model Fit Functions for saturated model

# Description

A general function that returns the model fit indices.

# Usage

TestFitSaturated(U, Z, ell\_A, nparam)

72 TestInformationFunc

#### **Arguments**

U is either a data class of exametrika, or raw data. When raw data is given, it is

converted to the exametrika class with the dataFormat function.

Z is a missing indicator matrix of the type matrix or data.frame

ell\_A log likelihood of this model

nparam number of parameters for this model

#### Value

model\_log\_like log likelihood of analysis model

bench\_log\_like log likelihood of benchmark model

null\_log\_like log likelihood of null model

model\_Chi\_sq Chi-Square statistics for analysis model

null\_Chi\_sq Chi-Square statistics for null model

model\_df degrees of freedom of analysis model

null\_df degrees of freedom of null model

**NFI** Normed Fit Index. Lager values closer to 1.0 indicate a better fit.

RFI Relative Fit Index. Lager values closer to 1.0 indicate a better fit.

**IFI** Incremental Fit Index. Lager values closer to 1.0 indicate a better fit.

TLI Tucker-Lewis Index. Lager values closer to 1.0 indicate a better fit.

**CFI** Comparative Fit Index. Lager values closer to 1.0 indicate a better fit.

**RMSEA** Root Mean Square Error of Approximation. Smaller values closer to 0.0 indicate a better fit.

**AIC** Akaike Information Criterion. A lower value indicates a better fit.

CAIC Consistent AIC.A lower value indicates a better fit.

**BIC** Bayesian Information Criterion. A lower value indicates a better fit.

TestInformationFunc TIF for IRT

#### **Description**

Test Information Function for 4PLM

#### Usage

TestInformationFunc(params, theta)

## **Arguments**

params parameter matrix theta ability parameter TestStatistics 73

#### Value

Returns a numeric vector representing the test information at each ability level theta. The test information is the sum of item information functions for all items in the test:  $I_{test}(\theta) = \sum_{j=1}^{n} I_j(\theta)$ 

TestStatistics

Simple Test Statistics

# Description

Statistics regarding the total score.

# Usage

```
TestStatistics(U, na = NULL, Z = NULL, w = NULL)
```

# **Arguments**

U is a data matrix of the type matrix or data.frar
--

na argument specifies the numbers or characters to be treated as missing values.

Z is a missing indicator matrix of the type matrix or data.frame

w w is item weight vector

#### Value

**TestLength** Length of the test. The number of items included in the test.

SampleSize Sample size. The number of rows in the dataset.

Mean Average number of correct answers.

SEofMean Standard error of mean

Variance Variance

SD Standard Deviation

Skewness Skewness

Kurtosis Kurtosis

Min Minimum score

Max Max score

Range Range of score

Q1 First quartile. Same as the 25th percentile.

**Median** Median. Same as the 50th percentile.

**Q3** Third quartile. Same as the 75th percentile.

**IQR** Interquartile range. It is calculated by subtracting the first quartile from the third quartile.

Stanine see stanine

```
# using sample dataset
TestStatistics(J15S500)
```

74 tetrachoric

te:	tra	cho	ric

Tetrachoric Correlation

# Description

Tetrachoric Correlation is superior to the phi coefficient as a measure of the relation of an item pair. See Divgi, 1979; Olsson, 1979; Harris, 1988.

# Usage

```
tetrachoric(x, y)
```

## **Arguments**

x binary vector x

y binary vector y

## Value

Returns a single numeric value of class "exametrika" representing the tetrachoric correlation coefficient between the two binary variables. The value ranges from -1 to 1, where:

- 1 indicates perfect positive correlation
- -1 indicates perfect negative correlation
- 0 indicates no correlation

#### References

Divgi, D. R. (1979). Calculation of the tetrachoric correlation coefficient. Psychometrika, 44, 169–172.

Olsson, U. (1979). Maximum likelihood estimation of the polychoric correlation coefficient. Psychometrika,44, 443–460.

Harris, B. (1988). Tetrachoric correlation coefficient. In L. Kotz, & N. L. Johnson (Eds.), Encyclopedia of statistical sciences (Vol. 9, pp. 223–225). Wiley.

#### TetrachoricCorrelationMatrix

# Tetrachoric Correlation Matrix

# Description

Calculates the matrix of tetrachoric correlations between all pairs of items. Tetrachoric Correlation is superior to the phi coefficient as a measure of the relation of an item pair. This function is applicable only to binary response data.

# Usage

```
TetrachoricCorrelationMatrix(U, na = NULL, Z = NULL, w = NULL, ...)
```

# **Arguments**

U	U is a data matrix of the type matrix or data.frame.
na	na argument specifies the numbers or characters to be treated as missing values.
Z	Z is a missing indicator matrix of the type matrix or data.frame
W	w is item weight vector
	Internal parameters for maintaining compatibility with the binary data processing system. Not intended for direct use.

#### Value

A matrix of tetrachoric correlations with exametrika class. Each element (i,j) represents the tetrachoric correlation between items i and j. The matrix is symmetric with ones on the diagonal.

# Note

This function is implemented using a binary data compatibility wrapper and will raise an error if used with polytomous data.

```
# example code
TetrachoricCorrelationMatrix(J15S500)
```

76 TwoPLM

ThreePLM	Three-Parameter Logistic Model	

# Description

The three-parameter logistic model is a model where the lower asymptote parameter c is added to the 2PLM

## Usage

```
ThreePLM(a, b, c, theta)
```

# **Arguments**

a	slope parameter
b	location parameter
С	lower asymptote parameter
theta	ability parameter

# Value

Returns a numeric vector of probabilities between c and 1, representing the probability of a correct response given the ability level theta. The probability is calculated using the formula:  $P(\theta) = c + \frac{1-c}{1+e^{-a(\theta-b)}}$ 

TwoPLM	Two-Parameter Logistic Model

# Description

The two-parameter logistic model is a classic model that defines the probability of a student with ability theta successfully answering item j, using both a slope parameter and a location parameter.

# Usage

```
TwoPLM(a, b, theta)
```

а	slope parameter
b	location parameter
theta	ability parameter

TwoPLM 77

# Value

Returns a numeric vector of probabilities between 0 and 1, representing the probability of a correct response given the ability level theta. The probability is calculated using the formula:  $P(\theta) = \frac{1}{1+e^{-\alpha(\theta-b)}}$ 

# **Index**

* datasets  J12S5000, 34  J15S500, 35  J20S400, 35  J35S515, 36  J5S10, 36  AlphaCoefficient, 3  AlphaIfDel, 4	ItemThreshold, 32 ItemTotalCorr, 33 J12S5000, 34 J15S500, 35 J20S400, 35 J35S515, 36 J5S10, 36 JCRR, 37
asymprior, 5	JointSampleSize, 38
Biclustering, 5, 56 BINET, 7 Biserial_Correlation, 10 BitRespPtn, 11 BNM, 11	LCA, 38, 56 LD_param_est, 45 LDB, 40, 56 LDLRA, 43 LogisticModel, 46
<pre>calcFitIndices, 13 CCRR, 14 crr, 15 CTT, 16</pre>	LRA, 46, 56  maxParents_penalty, 48  MutualInformation, 49
dataFormat, 6, 8, 12, 16, 23, 24, 28, 39, 40, 43, 47, 63, 65, 67, 71, 72 dataFormat.long, 17	nrs, 50  objective_function_IRT, 51 OmegaCoefficient, 51
Dimensionality, 19 FieldAnalysis, 19	passage, 52 percentile, 53 PhiCoefficient, 54
IIF2PLM, 20 IIF3PLM, 20 InterItemAnalysis, 21 IRM, 22	plot.exametrika, 6, 8, 23, 24, 39, 41, 47, 55 print.exametrika, 57 PSD_item_params, 58
IRT, 24, 55, 56	RaschModel, 59
ITBiserial, 26 ItemEntropy, 27 ItemFit, 25, 28, 39, 47 ItemInformationFunc, 29 ItemLift, 29 ItemOdds, 30 ItemStatistics, 31	slopeprior, 59 softmax, 60 sscore, 60 stanine, 61, 73 StrLearningGA_BNM, 63 StrLearningPBIL_BNM, 65

INDEX 79

```
StrLearningPBIL_LDLRA, 67
StudentAnalysis, 69

TestFit, 6, 9, 12, 24, 25, 39, 41, 44, 47, 64, 66, 69, 70

TestFitSaturated, 71
TestInformationFunc, 72
TestStatistics, 73
tetrachoric, 74
TetrachoricCorrelationMatrix, 75
ThreePLM, 76
TwoPLM, 76
```