Package 'mpt'

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Description Fitting and testing multinomial processing tree (MPT) models, a class of nonlinear models for categorical data. The parameters are the link probabilities of a tree-like graph and represent the latent cognitive processing steps executed to arrive at observable response categories (Batchelder & Riefer, 1999 <doi:10.3758 bf03210812="">; Erdfelder et al., 2009 <doi:10.1027 0044-3409.217.3.108="">; Riefer & Batchelder, 1988 <doi:10.1037 0033-295x.95.3.318="">).</doi:10.1037></doi:10.1027></doi:10.3758>
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Description

In a city-size paired-comparison task on each trial, participants judge which of two cities is more populous. After the paired comparisons, participants indicate for each city if they recognize its name. Hilbig, Erdfelder, and Pohl (2010) report a series of experiments to evaluate their model of recognition heuristic use at this task.

The WorldCities data are from a study designed to be similar to Hilbig et al.'s Experiment 6. The 17 cities were (in order of population; Wikipedia, 2016): Shanghai, Tianjin, Tokyo, Seoul, London, Bangkok, Chongqing, Wuhan, Santiago, Rangun, Ankara, Harbin, Kano, Busan, Durban, Ibadan, Montreal.

The ItalianCities data are from a study designed to be similar to Hilbig et al.'s Experiment 7. The 14 cities were: Milan, Naples, Turin, Palermo, Venice, Padua, Taranto, Prato, Reggio Emilia, Perugia, Cagliari, Foggia, Salerno, Ferrara.

Usage

data(citysize)

Format

WorldCities A data frame containing 37 observations of six variables:

gender factor. Participant gender.

age participant age.

rt median response time (in seconds) across paired comparisons.

group factor. The control group (CG) received standard instructions, the experimental group (EG) was instructed to choose the city they recognized whenever possible.

country number of cities whose country was correctly identified.

y a matrix of aggregate response frequencies per participant. The column names indicate each of eight response categories: correct/false responses when both cities were recognized (KC, KF), when both were unrecognized (GC, GF), when only one was recognized and the recognized city was chosen (RC, RF), and when only one was recognized and the unrecognized city was chosen (UF, UC).

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ItalianCities A data frame containing 64 observations of six variables:

```
gender, age, rt, y see above.
```

group factor. The control group (CG) received standard instructions, the experimental group (EG) was asked to compare the cities with respect to their elevation above sea level.

knowRH factor. Does the participant have any knowledge about the recognition heuristic (RH)?

Source

The WorldCities data were collected at the Department of Psychology, University of Tuebingen, in June/July 2016. The ItalianCities data are from Rettich (2020). The original data are from Castela et al. (2014).

References

Hilbig, B.E., Erdfelder, E., & Pohl, R.F. (2010). One-reason decision-making unveiled: A measurement model of the recognition heuristic. *Journal of Experimental Psychology: Learning, Memory, and Cognition*, **36**(1), 123–134. doi: 10.1037/a0017518

Castela, M., Kellen, D., Erdfelder, E., & Hilbig, B.E. (2014). The impact of subjective recognition experiences on recognition heuristic use: A multinomial processing tree approach. *Psychonomic Bulletin & Review*, **21**(5), 1131–1138. doi: 10.3758/s1342301405874

Rettich, A. (2020). Application of the recognition heuristic: An experimental validation of the r-model. Bachelor thesis. University of Tuebingen, Germany. https://osf.io/mz47y/

Wikipedia. (2016). List of cities proper by population. Retrieved Jun 16 from https://en.wikipedia.org/wiki/List_of_cities_proper_by_population.

See Also

mpt.

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```
unname(ItalianCities[ItalianCities$group == "EG", "y"]))
## Test task effect on r parameter
city.agg <- aggregate(y ~ group, ItalianCities, sum)</pre>
y <- as.vector(t(city.agg[, -1]))</pre>
m3 <- mpt(mptspec("rmodel", .replicates = 2), y)</pre>
m4 <- mpt(update(m1$spec, .restr = list(r2=r1)), y)</pre>
anova(m4, m3) # less use of RH with elevation task
## Plot parameter estimates
par(mfrow = 1:2)
dotchart(coef(m1)[c(4, 1:3)], xlim=0:1, labels=c("a", "b", "g", "r"),
         xlab="", main="by instruction type")
points(coef(m1)[c(8, 5:7)], 1:4, pch=16)
legend(0, 1, c("none", "recognition"), pch=c(1, 16),
       title="Instruction", bty="n")
dotchart(coef(m3)[c(4, 1:3)], xlim=0:1, labels=c("a", "b", "g", "r"),
         xlab="", main="by task type")
points(coef(m3)[c(8, 5:7)], 1:4, pch=16)
legend(0, 1, c("population", "elevation"), pch=c(1, 16),
       title="Task", bty="n")
title("Recognition heuristic use", outer=TRUE, line=-1)
mtext("Parameter estimate (r-model)", side=1, outer=TRUE, line=-2)
## Compare with original results
Hilbig2010 <- rbind(</pre>
    WorldCities.CG = c(462, 204, 290, 272, 740, 205, 77, 62),
    WorldCities.EG = c(500, 307, 279, 264, 902, 235, 68, 29),
  ItalianCities.CG = c(232, 78, 135, 136, 465, 65, 56, 16),
  ItalianCities.EG = c(245, 176, 154, 150, 228, 160, 112, 140)
)
apply(Hilbig2010, 1, mpt, spec = mptspec("rmodel"))
```

logLik.mpt

Log-Likelihood of an mpt Object

Description

Returns the log-likelihood value of the (joint) multinomial processing tree model represented by object evaluated at the estimated parameters.

Usage

```
## S3 method for class 'mpt'
logLik(object, ...)
```

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Arguments

object	an object inheriting from class mpt, representing a fitted multinomial processing tree model.
• • •	some methods for this generic require additional arguments. None are used in this method.

Value

The log-likelihood of the model represented by object evaluated at the estimated parameters.

See Also

```
mpt, logLik.lm, AIC, deviance, nobs.
```

Examples

```
m <- mpt(mptspec("SR2"), c(243, 64, 58, 55)) # from Riefer et al. (2002)
logLik(m)
deviance(m)
AIC(m)
AIC(m, k = log(sum(m$y))) # BIC w/total number of data points
BIC(m) # BIC using nobs()
nobs(m) # number of non-redundant response categories</pre>
```

moraldilemma

Moral Dilemma Judgment

Description

Hennig and Huetter (2020) proposed a multinomial model of moral dilemma judgment and evaluated the model in a series of experiments. Participants were presented with hypothetical scenarios that required a decision whether or not to break a moral norm.

Berentelg (2020) conducted a replication study that was designed to be similar to Experiment 2b in Hennig and Huetter (2020).

Usage

```
data(moraldilemma)
```

Format

MDHennig2020 A data frame consisting of seven variables:

selfrel factor. Instructions about self-relevant consequences of the decision where either (absent) or (present).

congrey factor. Endorsement of consequences and norm endorsement lead to different decisions (incongruent) or to the same decision (congruent).

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default factor. The norm may be adhered to by continuing (inaction default state) or by changing (action default state) an ongoing behavior.

breaknorm factor. Decision to break the norm.

exp1, exp2b the aggregate response frequencies for Experiment 1 and 2b, respectively.

treeid an identifier for the single trees of the joint multinomial model.

MDreplication A data frame containing 751 observations of five variables:

```
selfrel factor. See above.
```

gender factor. Participant gender.

age participant age.

rt median response time (in seconds) across scenarios.

y a matrix of response frequencies per participant. Each column represents a combination of the factors congrey, default, and breaknorm.

Source

Hennig, M., & Huetter, M. (2020). Revisiting the divide between deontology and utilitarianism in moral dilemma judgment: A multinomial modeling approach. *Journal of Personality and Social Psychology* **118**(1), 22–56. doi: 10.1037/pspa0000173

Berentelg, M. (2020). *Multinomial modeling of moral dilemma judgment: A replication study*. Bachelor thesis. University of Tuebingen, Germany. https://osf.io/mb32t/

See Also

mpt.

```
data(moraldilemma)
## Exp. 1: proCNI and process dissociation (PD) model
s <- mptspec("proCNI")</pre>
exp1 <- subset(MDHennig2020, selfrel == "absent")</pre>
mpt(update(s, .restr = list(I=0, J=1)), data = exp1, freqvar = "exp1")
## Exp. 2b: self-relevant consequences and norm endorsement
s <- mptspec("proCNI", .replicates = 2, .restr = list(J1=I1, J2=I2))</pre>
m1 <- mpt(s, data = MDHennig2020, freqvar = "exp2b")</pre>
m2 <- mpt(update(m1$spec, .restr = list(N1=N2)), data = m1$y)</pre>
anova(m2, m1)
## Replication of Exp. 2b
md.agg <- aggregate(y ~ selfrel, MDreplication, sum)</pre>
y <- as.vector(t(md.agg[, -1]))</pre>
m3 \leftarrow mpt(s, data = y)
m4 <- mpt(update(s, .restr = list(N1=N2)), data = y)</pre>
```

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mpt

Multinomial Processing Tree (MPT) Models

Description

Fits a (joint) multinomial processing tree (MPT) model specified by a symbolic description via mptspec.

Usage

```
mpt(spec, data, start = NULL, method = c("BFGS", "EM"), treeid = "treeid",
    freqvar = "freq", optimargs =
        if(method == "BFGS") list(control =
            list(reltol = .Machine$double.eps^(1/1.2), maxit = 1000))
        else list())

## S3 method for class 'mpt'
anova(object, ..., test = c("Chisq", "none"))

## S3 method for class 'mpt'
coef(object, logit = FALSE, ...)

## S3 method for class 'mpt'
confint(object, parm, level = 0.95, logit = TRUE, ...)

## S3 method for class 'mpt'
predict(object, newdata = NULL, type = c("freq", "prob"), ...)

## S3 method for class 'mpt'
summary(object, ...)
```

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Arguments

an object of class mptspec: typically result of a call to mptspec. A symbolic spec description of the model to be fitted. (See Details and Examples.) data a data frame consisting at least of one variable that contains the absolute response frequencies. Alternatively, a (named) vector or matrix of frequencies. start a vector of starting values for the parameter estimates between zero and one. method optimization method. Implemented are optim(..., method = "BFGS") and the EM algorithm. treeid name of the variable that identifies the processing trees of a joint multinomial model. Alternatively, a factor that identifies each tree. freqvar if data is a data frame, name of the variable that holds the response frequencies; else ignored. logit logical. Parameter estimates on logit or probability scale. a list of arguments passed to the optimization function, either optim or mptEM. optimargs object an object of class mpt, typically the result of a call to mpt. should the p-values of the chi-square distributions be reported? test See confint.default. parm, level a vector of response frequencies. newdata type predicted frequencies or probabilities. additional arguments passed to other methods.

Details

. . .

Multinomial processing tree models (Batchelder & Riefer, 1999; Erdfelder et al., 2009; Riefer & Batchelder, 1988) seek to represent the categorical responses of a group of subjects by a small number of latent (psychological) parameters. These models have a tree-like graph, the links being the parameters, the leaves being the response categories. The path from the root to one of the leaves represents the cognitive processing steps executed to arrive at a given response.

If data is a data frame, each row corresponds to one response category. If data is a vector or matrix, each element or column corresponds to one response category. The order of response categories and of model equations specified in mptspec should match.

Joint (or product) multinomial models consist of more than one processing tree. The treeid should uniquely identify each tree.

Per default, parameter estimation is carried out by optim's BFGS method on the logit scale with analytical gradients; it can be switched to mptEM which implements the EM algorithm.

Value

An object of class mpt containing the following components:

coefficients a vector of parameter estimates. For extraction, the coef function is preferred.

loglik the log-likelihood of the fitted model.

nobs the number of nonredundant response categories. mpt 9

```
fitted
                   the fitted response frequencies.
goodness.of.fit
                   the goodness of fit statistic including the likelihood ratio fitted vs. saturated
                   model (G2), the degrees of freedom, and the p-value of the corresponding chi-
                   square distribution.
ntrees
                   the number of trees in a joint multinomial model.
                   the total number of observations per tree.
                   the vector of response frequencies.
                   the predicted probabilities for each response category.
pcat
                   a factor that identifies each tree.
treeid
                   structural constants passed to mptEM.
a, b, c
                   the MPT model specification returned by mptspec.
spec
                   the optimization method used.
method
                   the return value of the optimization function.
optim
```

References

Batchelder, W.H., & Riefer, D.M. (1999). Theoretical and empirical review of multinomial process tree modeling. *Psychonomic Bulletin & Review*, **6**(1), 57–86. doi: 10.3758/bf03210812

Erdfelder, E., Auer, T., Hilbig, B.E., Assfalg, A., Moshagen, M., & Nadarevic, L. (2009). Multinomial processing tree models: A review of the literature. *Zeitschrift fuer Psychologie*, **217**(3), 108–124. doi: 10.1027/00443409.217.3.108

Riefer, D.M., & Batchelder, W.H. (1988). Multinomial modeling and the measurement of cognitive processes. *Psychological Review*, **95**(3), 318–339. doi: 10.1037/0033295x.95.3.318

See Also

```
mptEM, mptspec, simulate.mpt, plot.mpt, residuals.mpt, logLik.mpt, vcov.mpt, optim.
```

```
## Storage-retrieval model for pair clustering (Riefer & Batchelder, 1988)
data(retroact)

spec <- mptspec(
    c*r,
    (1 - c)*u^2,
    2*(1 - c)*u*(1 - u),
    c*(1 - r) + (1 - c)*(1 - u)^2,
    u,
    1 - u
)

m <- mpt(spec, retroact[retroact$lists == 0, ])

summary(m)  # parameter estimates, goodness of fit
plot(m)  # residuals versus predicted values
confint(m)  # approximate confidence intervals</pre>
```

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mptEM

EM Algorithm for Multinomial Processing Tree Models

Description

Applies the EM algorithm to fit a multinomial processing tree model.

Usage

Arguments

theta	a vector of starting values for the parameter estimates.
data	a vector of absolute response frequencies.
a	a three-dimensional array representing the model structure.
b	a three-dimensional array representing the model structure.
С	a matrix of structural constants.
maxit	the maximum number of iterations.
tolerance	the convergence criterion; the iterations converge when $logLik - logLik.old < tolerance$.
stepsize	the step size defaulting to 1; slightly larger values may speed up convergence, but may also give errors; use with care.
verbose	logical indicating if output should be produced for each iteration.

Details

Usually, mptEM is automatically called by mpt.

A prerequisite for the application of the EM algorithm is that the probabilities of the i-th branch leading to the j-th category take the form

$$p_{ij}(\Theta) = c_{ij} \prod_{s=1}^{S} \vartheta_s^{a_{ijs}} (1 - \vartheta_s)^{b_{ijs}},$$

where $\Theta = (\vartheta_s)$ is the parameter vector, a_{ijs} and b_{ijs} count the occurrences of ϑ_s and $1 - \vartheta_s$ in a branch, respectively, and c_{kj} is a nonnegative real number. The branch probabilities sum up to the

total probability of a given category, $p_j = p_{1j} + ... + p_{Ij}$. This is the structural restriction of the class of MPT models that can be represented by binary trees. Other model types have to be suitably reparameterized for the algorithm to apply.

See Hu and Batchelder (1994) and Hu (1999) for details on the algorithm.

Value

theta the vector of parameter estimates.

loglik the log-likelihood at termination of the algorithm.

pcat a vector of predicted probabilities for each response category.

pbranch a vector of predicted branch probabilities.

iter the number of iterations of the algorithm.

References

Hu, X. (1999). Multinomial processing tree models: An implementation. *Behavior Research Methods, Instruments, & Computers*, **31**(4), 689–695. doi: 10.3758/BF03200747

Hu, X., & Batchelder, W.H. (1994). The statistical analysis of general processing tree models with the EM algorithm. *Psychometrika*, **59**(1), 21–47. doi: 10.1007/bf02294263

See Also

mpt.

Examples

```
## Fit storage-retrieval model to data in Riefer et al. (2002)
mpt(mptspec("SR2"), c(243, 64, 58, 55), method = "EM")
```

mptspec

Specify a Multinomial Processing Tree (MPT) Model

Description

Returns the specification of an MPT model object for fitting with mpt.

Usage

```
mptspec(..., .replicates = NULL, .restr = NULL)
## S3 method for class 'mptspec'
update(object, .replicates = NULL, .restr = NULL, ...)
```

Arguments

.. (named) expressions or a character string specifying the model. See Details.

.replicates the number of replicates of the model equations. See Details.

. restr a named list of parameter restrictions. See Details.

object an object of class mptspec.

Details

. . . is used to symbolically specify the MPT model equations by suitable expressions, for example, they could look like this

$$r + (1 - r)*b$$
, $(1 - r)*(1 - b)$, b, 1 - b

where each expression represents the probability of a response in the corresponding category (link probabilities are multiplied, branch probabilities are added). Thus, there usually are as many expressions as response categories.

Joint (or product) multinomial models consist of more than a single processing tree. To identify the trees in such a model, expressions may have optional names. Canonically, these names are of the form x.y, where x is the tree identifier (treeid) and y specifies the response category within a tree.

Alternatively, ... may be a character string identifying one out of a list of pre-specified MPT models. Currently accessible are the following models (other models have to be specified by explicit expressions as described above):

1HT: the one-high-threshold model (Blackwell, 1963; Swets, 1961).

2HT: the two-high-threshold model (Snodgrass & Corwin, 1988; see also Broeder & Schuetz, 2009).

PairAsso: the paired-associate learning model (Riefer & Batchelder, 1988).

proCNI: the CNI model of moral dilemma judgment for proscriptive norms (Hennig & Huetter, 2020). The general formula includes the process dissociation (PD) model (Conway & Gawronski, 2013) as a special case.

prospec: the event-based prospective memory model (Smith & Bayen, 2004).

rmodel: the r-model of recognition heuristic use (Hilbig, Erdfelder, & Pohl, 2010).

SourceMon: the source-monitoring model (Batchelder & Riefer, 1990).

SR, SR2: the storage-retrieval model for pair clustering (Batchelder & Riefer, 1986). SR2 is the model without singleton items.

WST: the inference-guessing model with relaxed assumptions (Klauer, Stahl, & Erdfelder, 2007) for the Wason selection task.

The intended use of .replicates is to specify the number of replicates of the model equations, for example, when the same model is repeatedly applied in several experimental conditions. Accordingly, parameter names are augmented by numbers to make them unique.

Parameter restrictions included in .restr may be of the form b = r or b = 0.5 etc. Depending on the fitting algorithm employed in mpt (BFGS, but not EM), mathematical functions are permissible, for example, b = sqrt(r).

The update method is used to add parameter restrictions or replicates to an existing mptspec object.

Value

An object of class mptspec that serves as input to mpt which fits the model to data. It consists of the following components:

par2prob a function that takes a vector of parameter values and computes the response

probabilities.

par2deriv a function that takes a vector of parameter values and computes first and second

derivatives of the model equations.

prob a list containing expressions of the model equations.

deriv a list containing expressions of the first and second derivatives of the model

equations.

par a named vector of parameter values.

replicates the number of replicates of the model equations.

restr a list containing expressions of parameter restrictions.

treeid a factor that identifies each tree.

References

Batchelder, W.H., & Riefer, D.M. (1986). The statistical analysis of a model for storage and retrieval processes in human memory. *British Journal of Mathematical and Statistical Psychology*, **39**(2), 129–149. doi: 10.1111/j.20448317.1986.tb00852.x

Batchelder, W.H., & Riefer, D.M. (1990). Multinomial processing models of source monitoring. *Psychological Review*, **97**(4), 548–564. doi: 10.1037/0033295x.97.4.548

Blackwell, H.R. (1963). Neural theories of simple visual discriminations. *Journal of the Optical Society of America*, **53**(1), 129–160. doi: 10.1364/JOSA.53.000129

Broeder, A., & Schuetz, J. (2009). Recognition ROCs are curvilinear—or are they? On premature arguments against the two-high-threshold model of recognition. *Journal of Experimental Psychology: Learning, Memory, and Cognition*, **35**(3), 587–606. doi: 10.1037/a0015279

Conway, P., & Gawronski, B. (2013). Deontological and utilitarian inclinations in moral decision making: A process dissociation approach. *Journal of Personality and Social Psychology*, **104**(2), 216–235. doi: 10.1037/a0031021

Hennig, M., & Huetter, M. (2020). Revisiting the divide between deontology and utilitarianism in moral dilemma judgment: A multinomial modeling approach. *Journal of Personality and Social Psychology* **118**(1), 22–56. doi: 10.1037/pspa0000173

Hilbig, B.E., Erdfelder, E., & Pohl, R.F. (2010). One-reason decision-making unveiled: A measurement model of the recognition heuristic. *Journal of Experimental Psychology: Learning, Memory, and Cognition*, **36**(1), 123–134. doi: 10.1037/a0017518

Klauer, K.C., Stahl, C., & Erdfelder, E. (2007). The abstract selection task: New data and an almost comprehensive model. *Journal of Experimental Psychology: Learning, Memory, and Cognition*, **33**(4), 680–703. doi: 10.1037/02787393.33.4.680

Riefer, D.M., & Batchelder, W.H. (1988). Multinomial modeling and the measurement of cognitive processes. *Psychological Review*, **95**(3), 318–339. doi: 10.1037/0033295x.95.3.318

Smith, R.E., & Bayen, U.J. (2004). A multinomial model of event-based prospective memory. *Journal of Experimental Psychology: Learning, Memory, and Cognition*, **30**(4), 756–777. doi: 10.1037/02787393.30.4.756

Snodgrass, J.G., & Corwin, J. (1988). Pragmatics of measuring recognition memory: Applications to dementia and amnesia. *Journal of Experimental Psychology: General*, **117**(1), 34–50. doi: 10.1037/00963445.117.1.34

Swets, J. A. (1961). Is there a sensory threshold? *Science*, **134**(3473), 168–177. doi: 10.1126/science.134.3473.168

See Also

mpt.

```
## Specify storage-retrieval model for pairs
spec1 <- mptspec(</pre>
 c*r,
 (1 - c)*u^2,
 2*(1 - c)*u*(1 - u),
 c*(1 - r) + (1 - c)*(1 - u)^2
)
## Specify storage-retrieval model with parameter restrictions
spec2 <- mptspec(</pre>
 c*r,
 (1 - c)*u^2
 2*(1 - c)*u*(1 - u),
 c*(1 - r) + (1 - c)*(1 - u)^2
  .restr = list(c = r/2, u = 0.3)
## Optional names identifying trees in joint MPT model
spec3 <- mptspec(</pre>
      Target.Hit = r + (1 - r)*b,
      Target.Miss = (1 - r)*(1 - b),
 Distractor.FA = b,
 Distractor.CR = 1 - b,
 .replicates = 3,
  .restr = list(r1 = r, r2 = r, r3 = r)
)
## Pre-specified one-high-threshold model
spec4 <- mptspec("1HT")</pre>
## Fit to data in Broeder and Schuetz (2009)
m \leftarrow mpt(spec4, c(55, 35, 45, 765))
## Working with the mptspec object
spec4par2prob(c(0.5, 0.1))
                                # response probabilities
spec4$par2deriv(coef(m))$deriv # Jacobian matrix at ML estimate
```

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```
## See data(package = "mpt") for application examples.
```

plot.mpt

Diagnostic Plot for MPT Models

Description

Plots MPT residuals against fitted values.

Usage

Arguments

x, object	an object of class mpt, typically the result of a call to mpt.
showNames	logical. Should the names of the residuals be plotted? Defaults to TRUE.
xlab, ylab	graphical parameters passed to plot.
type	the type of residuals which should be returned; the alternatives are: "deviance" (default) and "pearson".
	further arguments passed to or from other methods.

Details

The deviance residuals are plotted against the predicted response probabilities. If showNames is true, plotting symbols are the names of the residuals.

Value

For residuals, a named vector of residuals having as many elements as response categories.

See Also

```
mpt, residuals.glm.
```

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Examples

```
## Compare two constrained MPT models
data(proact)
spec <- mptspec(</pre>
 p1*q1*r1,
 p1*q1*(1 - r1),
 p1*(1 - q1)*r1,
 (1 - p1) + p1*(1 - q1)*(1 - r1),
 p2*q2*r2,
 p2*q2*(1 - r2),
 p2*(1 - q2)*r2,
 (1 - p2) + p2*(1 - q2)*(1 - r2),
 p3*q3*r3,
 p3*q3*(1 - r3),
 p3*(1 - q3)*r3,
  (1 - p3) + p3*(1 - q3)*(1 - r3)
)
m1 <- mpt(update(spec, .restr = list(p2=p1, p3=p1)),</pre>
          proact[proact$test == 1, ])
m2 <- mpt(update(spec, .restr = list(q2=q1, q3=q1)), m1$y)</pre>
par(mfrow = c(1, 2))
                                      # residuals versus fitted values
plot(m1, main = "p constrained", ylim = c(-3, 3.5)) # good fit
plot(m2, main = "q constrained", ylim = c(-3, 3.5)) # bad fit
sum(resid(m1)^2)
                                      # likelihood ratio G2
sum( resid(m1, "pearson")^2 )
                                      # Pearson X2
```

proact

Recall Frequencies for DaPolito's Experiment on Proactive Inhibition

Description

In DaPolito's experiment (Greeno, James, DaPolito, & Polson, 1978), 60 subjects were presented with lists of stimulus-response associates to be learned, followed by a test in which only the stimuli were presented and the responses had to be recalled. Stimuli consisted of three-letter syllables, responses of the numbers from 1 to 30, so list items looked like, say, ESI-12, JOK-3, MAL-8, etc. Part of the items had two responses (A-B, A-C), the control items had only a single correct response. If the recall of C responses is poorer than that of control items, then proactive inhibition has occurred, that is interference with the recall by information that has been learned earlier.

Riefer and Batchelder (1988) analyzed only the A-B and A-C items. They investigated how repeated A-B presentation affects the B and C recall, respectively. The responses were classified into four categories and pooled across subjects.

Usage

```
data(proact)
```

prospecMemory 17

Format

A data frame consisting of five variables:

```
test first or second test.
```

abpres the number of A-B presentations.

resp a factor giving the response category; BC both B and C responses are correctly recalled, Bc only B is recalled, bC only C is recalled, bc neither response is recalled.

freq the aggregate recall frequencies per condition.

treeid an identifier for the single trees of the joint multinomial model.

Source

Greeno, J.G., James, C.T., DaPolito, F, & Polson, P.G. (1978). Associative learning: A cognitive analysis. Englewood Cliffs, NJ: Prentice-Hall.

Riefer, D.M., & Batchelder, W.H. (1988). Multinomial modeling and the measurement of cognitive processes. *Psychological Review*, **95**(3), 318–339. doi: 10.1037/0033295x.95.3.318

See Also

mpt.

```
data(proact)
## Testing effects of repeated A-B presentations
spec <- mptspec(
    .BC = p*q*r,
    .Bc = p*q*(1 - r),
    .bC = p*(1 - q)*r,
    .bc = (1 - p) + p*(1 - q)*(1 - r),
    .replicates = 6
)
m1 <- mpt(spec, proact)
m2 <- mpt(update(spec, .restr = list(q2=q1, q3=q1, q5=q4, q6=q4)), proact)
m3 <- mpt(update(spec, .restr = list(r2=r1, r3=r1, r5=r4, r6=r4)), proact)
anova(m2, m1) # q increases with number of A-B presentations
anova(m3, m1) # r remains constant</pre>
```

18 prospecMemory

Description

Smith and Bayen (2004) tested the performance of 64 participants in an event-based prospective memory task that was embedded in a color-matching task. On each trial, participants were presented with four colored rectangles followed by a colored word. Their task was to press a key to indicate whether the color of the word matched one of the rectangles. Interspersed among these nontarget words were six target words for which subjects had to remember to press a special key (prospective memory response) regardless of the color. Participants received two different instruction types either stressing the importance of the color-matching (CMI) or of the prospective-memory task (PMI).

In a replication study, the performance of 72 German-speaking participants was tested; this study was designed to be similar to Experiment 1 in Smith and Bayen (2004).

Usage

data(prospecMemory)

Format

PMSmithBayen A data frame consisting of five variables:

instruction instruction type, either color-matching importance (cmi) or prospective memory importance (pmi).

item a factor specifying one of four item types: either a target word that did or did not match the color of the rectangles, or a nontarget word that did or did not match.

resp a factor giving the response categories: match, nonmatch, or the prospective memory response (prospec).

freq the aggregate response frequencies per condition.

treeid an identifier for the single trees of the joint multinomial model.

PMreplication A data frame containing 72 observations of five variables:

gender factor. Participant gender.

age participant age.

instr factor. Instruction type.

rtdiff average response time difference (in milliseconds) between color-matching and prospective-memory task.

y a matrix of aggregate response frequencies per participant. The column names indicate each of twelve response categories: match, nonmatch, prospective memory response for targets in matching (tmm, tmn, tmp) or in nonmatching condition (tnm, tnn, tnp), and again for nontargets (nmm, nmn, nmp vs. nnm, nnn, nnp).

Source

Smith, R.E., & Bayen, U.J. (2004). A multinomial model of event-based prospective memory. *Journal of Experimental Psychology: Learning, Memory, and Cognition*, **30**(4), 756–777. doi: 10.1037/02787393.30.4.756

For the replication study, data were collected at the Department of Psychology, University of Tuebingen, between December 2018 and January 2019. prospecMemory 19

See Also

mpt.

```
## Prospective memory model: identifiability
qr(mptspec("prospec",
   .restr = list(M1=M, M2=M))$par2deriv(runif(6))$deriv)$rank
qr(mptspec("prospec",
   .restr = list(M1=M, M2=M, g=.1, c=.5))par2deriv(runif(4))deriv)rank
## Prospective memory model: goodness of fit
data(prospecMemory)
cmi <- PMSmithBayen[PMSmithBayen$instruction == "cmi", ]</pre>
m2 <- mpt(mptspec("prospec", .restr = list(M1=M, M2=M, g=.1, c=.5)), cmi)</pre>
m1 <- mpt(update(m2$spec, .restr = list(C2=C1)), cmi)</pre>
anova(m1, m2)
pmi <- PMSmithBayen[PMSmithBayen$instruction == "pmi", ]</pre>
anova(mpt(m1$spec, pmi), mpt(m2$spec, pmi))
## Testing P_cmi = P_pmi and M_cmi = M_pmi
## Smith and Bayen
m2 <- mpt(mptspec("prospec", .replicates = 2,</pre>
                   .restr = list(M11=M1, M21=M1, g1=.1, c1=.5,
                                 M12=M2, M22=M2, g2=.1, c2=.5)),
          data = PMSmithBayen)
m1 <- mpt(update(m2$spec, .restr = list(P2=P1)), PMSmithBayen)</pre>
m0 <- mpt(update(m2$spec, .restr = list(M2=M1)), PMSmithBayen)</pre>
anova(m1, m2)
anova(m0, m2)
## Replication
pm.agg <- aggregate(y ~ instr, PMreplication, sum)</pre>
y <- as.vector(t(pm.agg[2:1, -1]))</pre>
m3 \leftarrow mpt(m2\$spec, y)
m1 <- mpt(update(m3$spec, .restr = list(P2=P1)), y)</pre>
m0 <- mpt(update(m3$spec, .restr = list(M2=M1)), y)</pre>
anova(m1, m3)
anova(m0, m3)
par(mfrow = 1:2)
dotchart(coef(m2)[c("C12", "C22", "P2", "M2")], xlim=0:1, xlab="",
  labels=c("C1", "C2", "P", "M"), main="Smith and Bayen (2004, Exp. 1)")
points(coef(m2)[c("C11", "C21", "P1", "M1")], 1:4, pch=16)
legend("bottomleft", c("CMI", "PMI"), pch=c(1, 16), title="Instruction",
       title.adj=1, bty="n")
dotchart(coef(m3)[c("C12", "C22", "P2", "M2")], xlim=0:1, xlab="",
  labels=c("C1", "C2", "P", "M"), main="Replication study")
```

20 recogROC

recogR0C

Recognition Receiver Operating Characteristics

Description

In a series of experiments, Broeder and Schuetz (2009) tested the shape of recognition receiver operating characteristics. Participants studied a list of items. In a recognition test, old items intermixed with new ones were presented, and participants had to classify them as old or new. The percentage of old items varied in order to manipulate the response bias.

Wellingerhof (2019) conducted a replication study that was designed to be similar to Experiment 3 in Broeder and Schuetz (2009).

Usage

data(recogROC)

Format

ROCBroeder2009 A data frame consisting of seven variables:

item factor. Target (old) or distractor (new) item.

resp a factor giving the response category, old or new.

treeid an identifier for the single trees of the joint multinomial model.

ptarget1, ptarget3 percentage of target (old) items in Experiment 1 and 3, respectively.

exp1, exp3 the aggregate response frequencies.

ROCreplication A data frame containing 48 observations of five variables:

gender factor. Participant gender.

age participant age.

arith number of mental-arithmetic problems solved.

lexical number of correct trials in lexical selection task.

y a matrix of aggregate response frequencies per participant. The column names indicate each of 4 x 5 response categories: hit, miss, false alarm, and correct rejection in the five bias conditions.

Source

Broeder, A., & Schuetz, J. (2009). Recognition ROCs are curvilinear—or are they? On premature arguments against the two-high-threshold model of recognition. *Journal of Experimental Psychology: Learning, Memory, and Cognition*, **35**(3), 587–606. doi: 10.1037/a0015279

Wellingerhof, P. (2019). Signal detection theory vs. 2-high-threshold model in recognition memory: A preregistered replication study. Bachelor thesis. University of Tuebingen, Germany. https://osf.io/hvg4p/

retroact 21

See Also

mpt.

Examples

```
data(recogROC)
## Two-high-threshold model
s <- mptspec("2HT", .replicates = 5,</pre>
                    .restr = list(r1=r, r2=r, r3=r, r4=r, r5=r,
                                 d1=d, d2=d, d3=d, d4=d, d5=d))
m1 <- mpt(s, data = ROCBroeder2009, freqvar = "exp3")</pre>
m2 <- mpt(s, data = unname(ROCreplication$y))</pre>
## Table 4
rbind(Broeder2009 = c(deviance(m1), coef(m1)),
      Replication = c(deviance(m2), coef(m2)))
## Hit rate and false alarm rate
i.hit <- with(ROCBroeder2009, item == "target" & resp == "old")
i.fa <- with(ROCBroeder2009, item == "distractor" & resp == "old")
hrfa <- data.frame(</pre>
   study = rep(c("Broeder2009", "Replication"), each=5),
   obshr = c((m1\$y/m1\$n)[i.hit], (m2\$y/m2\$n)[i.hit]),
   obsfa = c((m1\$y/m1\$n)[i.fa], (m2\$y/m2\$n)[i.fa]),
  predfa = c(m1$pcat[i.fa],
                                m2$pcat[i.fa])
)
## ROC, Figure 7
plot(obshr ~ obsfa, hrfa[hrfa$study == "Broeder2009", ],
     xlim=0:1, ylim=0:1, pch=16,
     main="Linear recognition ROCs?",
     ylab="Hit rate", xlab="False alarm rate")
abline(0, 1, lty=2)
lines(predhr ~ predfa, hrfa[hrfa$study == "Broeder2009", ])
points(obshr ~ obsfa, hrfa[hrfa$study == "Replication", ], col = "blue")
lines(predhr ~ predfa, hrfa[hrfa$study == "Replication", ],
      col = "blue")
text(0.45, 0.93, "Replication", col = "blue")
text(0.59, 0.82, "Broeder and Schuetz\n(2009, Exp. 3)")
```

retroact

Recall Frequencies in Retroactive Inhibition

Description

Riefer and Batchelder (1988) presented each of 75 participants with either one, two, three, four, or five successive lists of words (15 subjects per group). These words were shown in random order

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on a computer screen, one word at a time, at a rate of 5 s per word. Each list contained 25 words, consisting of 10 categories (with 2 associate words per category) and five singletons. Subjects were given 1.5 min to recall in writing the 25 words from each individual list. After all of the lists had been presented, a final free-recall test was given in which subjects attempted to recall the words from all of the previous lists. Subjects were given up to 5 min for this final written recall.

The focus here is on the recall of the first-list words during the final recall task. The responses were classified into six categories and pooled across subjects.

Usage

```
data(retroact)
```

Format

A data frame consisting of four variables:

lists the number of interpolated lists.

treeid an identifier for the single trees of the joint multinomial model.

resp a factor giving the response category; E1 pair is recalled adjacently, E2 pair is recalled non-adjacently, E3 one word in a pair is recalled, E4 neither word in a pair is recalled, F1 recall of a singleton, F2 non-recall of a singleton.

freq the aggregate recall frequencies per condition.

Source

Riefer, D.M., & Batchelder, W.H. (1988). Multinomial modeling and the measurement of cognitive processes. *Psychological Review*, **95**(3), 318–339. doi: 10.1037/0033295x.95.3.318

See Also

mpt.

```
data(retroact)
## Fitting individual storage-retrieval models per condition
spec <- mptspec(
    c*r,
    (1 - c)*u^2,
    2*(1 - c)*u*(1 - u),
    c*(1 - r) + (1 - c)*(1 - u)^2,
    u,
    1 - u
)
pars <- sapply(0:4,
    function(x) coef(mpt(spec, retroact[retroact$lists == x, ])))
## Figure 3 in Riefer & Batchelder (1988)
plot(pars["c", ] ~ I(0:4), pch=16, type="b", ylim=c(.3, 1),</pre>
```

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```
xlab="Number of interpolated lists, j",
     ylab="Parameter estimate (Storage-retrieval model)",
     main="Riefer and Batchelder (1988)")
points(pars["r", ] \sim I(0:4), type="b", lty=2)
text(3, .89, expression("Storage of clusters," ~ hat(c)[j]))
text(3, .46, expression("Retrieval of clusters," ~ hat(r)[j]))
## Testing effects of interpolated lists
spec <- mptspec(</pre>
  c0*r0,
  (1 - c0)*u0^2,
  2*(1 - c0)*u0*(1 - u0),
  c0*(1 - r0) + (1 - c0)*(1 - u0)^2
  u0,
  1 - u0,
  c1*r1,
  (1 - c1)*u1^2
  2*(1 - c1)*u1*(1 - u1),
  c1*(1 - r1) + (1 - c1)*(1 - u1)^2
  u1,
  1 - u1,
  c2*r2,
  (1 - c2)*u2^2,
  2*(1 - c2)*u2*(1 - u2),
  c2*(1 - r2) + (1 - c2)*(1 - u2)^2,
  u2,
  1 - u2,
  c3*r3,
  (1 - c3)*u3^2,
  2*(1 - c3)*u3*(1 - u3),
  c3*(1 - r3) + (1 - c3)*(1 - u3)^2,
  u3,
  1 - u3,
  c4*r4,
  (1 - c4)*u4^2,
  2*(1 - c4)*u4*(1 - u4),
  c4*(1 - r4) + (1 - c4)*(1 - u4)^2
 u4,
  1 - u4
)
m1 <- mpt(spec, retroact)</pre>
m2 <- mpt(update(spec, .restr=list(r0=r, r1=r, r2=r, r3=r, r4=r)),</pre>
          retroact)
m3 <- mpt(update(spec, .restr=list(c0=c, c1=c, c2=c, c3=c, c4=c)),
          retroact)
anova(m2, m1) \# r decreases the more lists have been interpolated
anova(m3, m1) # c remains constant
```

24 selectiontask

selectiontask

Wason Selection Task (WST) and Helpful Hints

Description

In the Wason selection task, a participant is presented with four cards, each one having a letter side and a number side, e.g., A B 3 4. The task is to select the card(s) that have to be turned around in order to test the rule "If there is an A on the letter side then there is a 3 on the number side." Klauer, Stahl, and Erdfelder (2007) report a series of experiments to test their WST model using the aggregate frequencies of the 16 possible response patterns.

Bauder (2020) conducted a replication study that was designed to be similar to Experiment 1 in Klauer et al. (2007).

Usage

data(selectiontask)

Format

WSTKlauer2007 A data frame consisting of four variables:

group factor. The control group (CG) received standard instructions, the experimental group (EG) got additional helpful hints.

pattern character. Response pattern indicating which card(s) were selected (1) or not selected (0).

exp1, exp2 the aggregate response frequencies for Experiment 1 and 2, respectively.

WSTreplication A data frame containing 1118 observations of eight variables:

status factor. Was the participant excluded?

group factor. The experimental group.

gender factor. Participant gender.

age participant age.

education years of education.

logic factor. Familiarity with formal logic.

time seconds spent on the web page.

y a participant by response pattern indicator matrix.

Note

In the original analyses (Klauer et al., 2007), a constant of one was added to all frequencies.

selectiontask 25

Source

Klauer, K.C., Stahl, C., & Erdfelder, E. (2007). The abstract selection task: New data and an almost comprehensive model. *Journal of Experimental Psychology: Learning, Memory, and Cognition*, **33**(4), 680–703. doi: 10.1037/02787393.33.4.680

Bauder, D. (2020). *Die Modellierung der abstrakten Auswahlaufgabe von Wason - eine Replikationsstudie*. Bachelor thesis. University of Tuebingen, Germany. https://osf.io/3z7ux/

See Also

mpt.

```
data(selectiontask)
## Inference-guessing model with relaxed assumptions
s <- mptspec("WST", .replicates = 2)</pre>
m1 <- mpt(s, data = WSTKlauer2007$exp1, method = "EM")</pre>
## Inference-guessing model
m2 <- mpt(update(s, .restr = list(sf1=s1, sb1=s1, sfb1=s1,</pre>
                                    sf2=s2, sb2=s2, sfb2=s2)),
          data = m1$y, method = "EM")
## Effect of hint on i parameter (Exp. 1)
m3 <- mpt(update(m2$spec, .restr = list(i2=i1)), data = m1$y,
          method = "EM")
## Independence model
m4 <- mpt(update(m2$spec,</pre>
                  .restr = list(a1=0, c1=0, x1=0, d1=0, s1=0, i1=0,
                                a2=0, c2=0, x2=0, d2=0, s2=0, i2=0)),
          data = m1\$y, method = "EM")
anova(m4, m3, m2, m1)
plogis(confint(m2))
AIC(m2)
BIC(m2) # BIC w/number of non-redundant response categories
AIC(m2, k = log(sum(m2$y))) # BIC w/total number of data points
## Effect of hint on c parameter (Exp. 2)
m5 <- mpt(m2$spec, data = WSTKlauer2007$exp2, method = "EM")</pre>
m6 <- mpt(update(m5$spec, .restr = list(c2=c1)), data = m5$y,</pre>
          method = "EM")
anova(m6, m5)
## Replication of Exp. 1
wst.agg <- aggregate(y ~ group, WSTreplication,</pre>
                      subset = status == "select", sum)
y <- as.vector(t(wst.agg[, -1]))</pre>
```

26 simulate.mpt

simulate.mpt

Simulate Responses from MPT Models

Description

Simulates responses from the distribution corresponding to a fitted mpt model object.

Usage

```
## S3 method for class 'mpt'
simulate(object, nsim, seed, pool = TRUE, ...)
```

Arguments

object an object of class mpt, typically the result of a call to mpt.

nsim, seed currently not used.

pool logical, if TRUE (default), pooled responses (summed across respondents) are

returned.

... further arguments passed to or from other methods. None are used in this

method.

Details

Responses are simulated by (repeatedly) applying rmultinom with sizes taken from the original sample and probabilities computed from the model object.

Value

A named vector of (pooled) responses. Names identify the tree from which responses were simulated.

valence 27

See Also

```
mpt, rmultinom.
```

Examples

valence

World Valence and Source Memory for Vertical Position

Description

Sixty-four participants studied words with positive, negative, or neutral valence displayed at the top or bottom part of a computer screen. Later, these words were presented intermixed with new words, and participants had to classify them as "top," "bottom," or "new." It was of interest if memory is improved in congruent trials, in which word valence and vertical position match (positive-top, negative-bottom), as opposed to incongruent trials.

Usage

```
data(valence)
```

Format

A data frame consisting of five components:

```
id factor. Participant ID.
gender factor. Participant gender.
age participant age.
```

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condition factor. In congruent trials, positive words were presented at the top, negative words at the bottom, and vice versa for incongruent trials.

y a matrix of aggregate response frequencies per participant and condition. The column names indicate each of nine response categories, for example, top.bottom means that words were presented at the top, but participant responded "bottom."

Source

Data were collected at the Department of Psychology, University of Tuebingen, in 2010.

See Also

mpt.

```
data(valence)
## Fit source-monitoring model to subsets of data
spec <- mptspec("SourceMon", .restr=list(d1=d, d2=d))</pre>
names(spec$prob) <- colnames(valence$y)</pre>
mpt(spec, valence[valence$condition == "congruent" &
                   valence$gender == "female", "y"])
mpt(spec, valence[valence$condition == "incongruent" &
                   valence$gender == "female", "y"])
## Test the congruency effect
val.agg <- aggregate(y ~ gender + condition, valence, sum)</pre>
y <- as.vector(t(val.agg[, -(1:2)]))</pre>
spec <- mptspec("SourceMon", .replicates=4,</pre>
                 .restr=list(d11=d1, d21=d1, d12=d2, d22=d2,
                              d13=d3, d23=d3, d14=d4, d24=d4))
m1 <- mpt(spec, y)</pre>
m2 <- mpt(update(spec, .restr=list(d1=d.f, d3=d.f, d2=d.m, d4=d.m)), y)</pre>
anova(m2, m1) # better discrimination in congruent trials
## Plot parameter estimates
mat <- matrix(coef(m1), 5)</pre>
rownames(mat) <- c("D1", "d", "g", "b", "D2")
mat <- mat[c("D1", "D2", "d", "b", "g"), ]
matplot(mat, type="b", axes=FALSE, ylab="MPT model parameter estimate",
        main="Word valence and source monitoring", ylim=0:1, pch=1:4)
axis(1, 1:5, rownames(mat)); axis(2)
legend("bottomleft", c("female, congruent", "male, congruent",
        "female, incongruent", "male, incongruent"), pch=1:4, bty="n")
```

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vcov.mpt	Covariance and Information Matrix for MPT Models
----------	--

Description

Returns the covariance matrix or the Fisher information matrix of a fitted mpt model object.

Usage

```
## S3 method for class 'mpt'
vcov(object, logit = FALSE, what = c("vcov", "fisher"), ...)
```

Arguments

object an object of class mpt, typically the result of a call to mpt.

logit logical. Switch between logit and probability scale.

what character. If vcov (default), the covariance matrix is returned; if fisher, the

Fisher information matrix is returned.

... further arguments passed to or from other methods. None are used in this

method.

Details

If logit is false, the covariance matrix is based on the observed Fisher information matrix of the ML estimator on the probability scale. This is equivalent to the equations for the covariance matrix given in Hu and Batchelder (1994) and Hu (1999), although the implementation here is different.

If logit is true, the covariance matrix and the estimated information matrix (Elandt-Johnson, 1971) of the ML estimator on the logit scale are obtained by the multivariate delta method (Bishop, Fienberg, and Holland, 1975; Grizzle, Starmer, and Koch, 1969).

Value

A (named) square matrix.

References

Bishop, Y.M.M., Fienberg, S.E., & Holland, P.W. (1975). *Discrete multivariate analysis: Theory and practice*. Cambridge: MIT Press.

Elandt-Johnson, R. C. (1971). *Probability models and statistical methods in genetics*. New York: Wiley.

Grizzle, J.E., Starmer, C.F., & Koch, G. (1969). Analysis of categorical data by linear models. *Biometrics*, **25**(3), 489–504. doi: 10.2307/2528901

Hu, X. (1999). Multinomial processing tree models: An implementation. *Behavior Research Methods, Instruments, & Computers*, **31**(4), 689–695. doi: 10.3758/BF03200747

Hu, X., & Batchelder, W.H. (1994). The statistical analysis of general processing tree models with the EM algorithm. *Psychometrika*, **59**(1), 21–47. doi: 10.1007/bf02294263

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See Also

mpt.

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