## Package 'wqspt'

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Title Permutation Test for Weighted Quantile Sum Regression

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**Description** Implements a permutation test method for the weighted quantile sum (WQS) regression, building off the 'gWQS' package (Ren-

zetti et al. (2021) <a href="https://cran.re-project.org/package=gWQS">https://cran.re-project.org/package=gWQS></a>). Weighted quantile sum regression is a statistical technique to evaluate the effect of complex exposure mixtures on an outcome (Carrico et al. (2015) <a href="https://doi.org/10.1007/s13253-014-0180-3">doi:10.1007/s13253-014-0180-3</a>). The model features a statistical power and Type I error (i.e., false positive) rate trade-off, as there is a machine learning step to determine the weights that optimize the linear model fit. This package provides an alternative method based on a permutation test that should reliably allow for both high power and low false positive rate when utilizing WQS regression (Day et al. (2022) <a href="https://doi.org/10.1289/EHP10570">doi:10.1289/EHP10570</a>).

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wqspt\_plot

Plotting method for wqspt object

#### Description

Generates plots to help visualize and summarize WQS permutation test results.

#### Usage

```
wqspt_plot(
  wqsptresults,
  FixedPalette = FALSE,
  InclKey = FALSE,
  AltMixName = NULL,
  AltOutcomeName = NULL,
  ViridisPalette = "D",
  StripTextSize = 14,
  AxisTextSize.Y = 12,
  AxisTextSize.X = 12,
  LegendTextSize = 14,
  PvalLabelSize = 5,
  HeatMapTextSize = 5)
```

#### **Arguments**

wqsptresults	An object of class wqs_pt.
FixedPalette	If TRUE, the heatmap color key for the mixture weights has categorical cutoffs with the following categories: $<0.1$ , $0.1 - <0.2$ , $0.2 - <0.3$ , and $>=0.3$ . If false, the heatmap color key is continuous and dependent on the weight values.
InclKey	If TRUE, a horizontal heatmap legend is included at the bottom of the full plot.
AltMixName	Defaults to NULL. If not NULL, these are alternative names for the mixture components to be displayed on the heatmap y axis.
AltOutcomeName	Defaults to NULL. If not NULL, this is an alternative name for the outcome to be displayed on the heatmap x axis.
ViridisPalette	Color palette to be used for the viridisLite package-based coloring of the heatmap, with possible values from 'A' to 'E'. Defaults to 'D'.

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```
StripTextSize Text size for the plot strip labels. Defaults to 14.

AxisTextSize.Y Text size for the y axis text. Defaults to 12.

AxisTextSize.X Text size for the x axis text. Defaults to 12.

LegendTextSize Text text size for the legend text. Defaults to 14.

PvalLabelSize The geom_text size for the permutation test p-value label. Defaults to 5.

HeatMapTextSize
```

The geom\_text size for the mixture weight heatmap labels. Defaults to 5.

#### Value

Returns a list with 4 objects.

FullPlot	Two plots stacked vertically: (1) Forest plot of the beta WQS coefficient with the naive confidence intervals as well as the permutation test p-value (2) A heatmap of the WQS weights for each mixture component.
CoefPlot	Forest plot of the beta WQS coefficient with the naive confidence intervals as well as the permutation test p-value.
WtPlot	A heatmap of the WQS weights for each mixture component.
WtLegend	A legend for the weights in the WtPlot heatmap.

wqs_full_perm Full wrapper WQS permutation test
---

#### **Description**

wqs\_full\_perm is a full wrapper function that is a full implementation of the Weighted Quantile Sum (WQS) regression method followed by the permutation test to determine the significance of the WQS coefficient.

#### Usage

```
wqs_full_perm(
  formula,
  data,
  mix_name,
  q = 10,
  b_main = 1000,
  b_perm = 200,
  b1_pos = TRUE,
  b1_constr = FALSE,
  rs = FALSE,
  niter = 200,
  seed = NULL,
  family = "gaussian",
  plan_strategy = "multicore",
```

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```
stop_if_nonsig = FALSE,
stop_thresh = 0.05,
...
)
```

#### **Arguments**

formula An object of class formula. The wqs term must be included in the formula (e.g.,

 $y \sim wqs + ...$ ).

data The data. frame to be used in the WQS regression run.

mix\_name A vector with the mixture column names.

q An integer to indicate the number of quantiles to split the mixture variables.

b\_main The number of bootstraps for the main WQS regression run.

b\_perm The number of bootstraps for the iterated permutation test WQS regression runs

and the reference WQS regression run (only for linear WQS regression and only

when  $b_mean != b_perm$ ).

b1\_pos A logical value that indicates whether beta values should be positive or negative.

b1\_constr Logical value that determines whether to apply positive or negative constraints

in the optimization function for the weight optimization.

rs A logical value indicating whether random subset implementation should be

performed.

niter Number of permutation test iterations.

seed An integer to fix the seed. This will only impact the the initial WQS regression

run and not the permutation test iterations. The default setting is NULL, which means no seed is used for the initial WQS regression. The seed will be saved in

the "gwqs\_main" object as "gwqs\_main\$seed".

family A description of the error distribution and link function to be used in the model.

This can be a character string naming a family function (e.g., "binomial") or a family object (e.g., binomial(link="logit")). Currently validated families include gaussian(link="identity") for linear regression, binomial() with any accepted link function (e.g., "logit" or "probit"), poisson(link = "log"), quasipoisson(link = "log"), or "negbin" for negative binomial. The "multinomial" family

is not yet supported.

plan\_strategy Evaluation strategy for the plan function. You can choose among "sequen-

tial", "transparent", "multisession", "multicore", "multiprocess", "cluster" and

"remote." See future::plan documentation for full details.

stop\_if\_nonsig if TRUE, the function will not proceed with the permutation test if the main

WQS regression run produces nonsignificant p-value.

stop\_thresh numeric p-value threshold required in order to proceed with the permutation test,

if stop\_if\_nonsig = TRUE.

... Other parameters to put into the gwqs function call.

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#### Value

wqs\_full\_perm returns an object of class wqs\_perm, which contains three sublists:

perm\_test List containing: (1) pval: permutation test p-value, (2) (linear regression only) testbeta1: reference WQS regression coefficient beta1 value, (3) (linear regression only) betas: Vector of beta values from each permutation test run, (4) (logistic regression only) testpval: test reference p-value, (5) (logistic regression only) permpvals: p-values from the null models. Main gWQS object (same as model input). This will now include an additional gwqs\_main object "seed" that returns the seed used for this main WQS regression. Permutation test reference gWQS object (NULL if model family != "gaussian" gwqs\_perm

or if same number of bootstraps are used in permutation test WQS regression

runs as in the main run).

#### **Examples**

```
library(gWQS)
# mixture names
PCBs <- names(wqs_data)[1:17] #half of the original 34 for quick computation
perm_test_res <- wqs_full_perm(formula = yLBX ~ wqs, data = wqs_data,</pre>
                                mix_name = PCBs, q = 10, b_main = 5,
                                b_perm = 5, b1_pos = TRUE, b1_constr = FALSE,
                                niter = 3, seed = 16, plan_strategy = "multicore",
                                stop_if_nonsig = FALSE)
# Note: The default values of b_main = 1000, b_perm = 200, and niter = 200
# are the recommended parameter values. This example has a lower b_main,
# b_perm, and niter in order to serve as a shorter test run.
```

wqs\_pt

WQS permutation test

#### **Description**

wqs\_pt takes a gwqs object as an input and runs the permutation test (Day et al. 2022) to obtain an estimate for the p-value significance for the WQS coefficient.

### Usage

```
wqs_pt(
  model,
 niter = 200,
  boots = NULL,
 b1_pos = TRUE,
```

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```
b1_constr = FALSE,
  rs = FALSE,
  plan_strategy = "multicore",
  seed = NULL
)
```

#### **Arguments**

model A gwqs object as generated from the gWQS package.

niter Number of permutation test iterations.

Number of bootstrap samples for each permutation test WQS regression itera-

tion. If boots is not specified, then we will use the same bootstrap count for each permutation test WQS regression iteration as that specified in the main

WQS regression run.

b1\_pos A logical value that indicates whether beta values should be positive or negative.

b1\_constr Logical value that determines whether to apply positive or negative constraints

in the optimization function for the weight optimization.

rs A logical value indicating whether random subset implementation should be

performed.

plan\_strategy Evaluation strategy for the plan function. You can choose among "sequen-

tial", "transparent", "multisession", "multicore", "multiprocess", "cluster" and

"remote." See future::plan documentation for full details.

seed (optional) Random seed for the permutation test WQS reference run. This

should be the same random seed as used for the main WQS regression run.

This seed will be saved in the "gwqs\_perm" object as "gwqs\_perm\$seed".

#### **Details**

To use wqs\_pt, we first need to run an initial WQS regression run while setting validation = 0. We will use this gwqs object as the model argument for the wqs\_pt function. Note that permutation test has so far only been validated for linear WQS regression (i.e., family = "gaussian") or logistic WQS regression (i.e., family = binomial(link = "logit")), though the permutation test algorithm should also work for all WQS GLMs. Therefore, this function accepts gwqs objects made with the following families: "gaussian" or gaussian(link = "identity"), "binomial" or binomial() with any accepted link function (e.g., "logit" or "probit"), "poisson" or poisson(link="log"), "negbin" for negative binomial, and "quasipoisson" or quasipoisson(link="log"). This function cannot currently accommodate gwqs objects made with the "multinomial" family, and it is not currently able to accommodate stratified weights or WQS interaction terms (e.g., y ~ wqs \* sex).

The argument boots is the number of bootstraps for the WQS regression run in each permutation test iteration. Note that we may elect a bootstrap count boots lower than that specified in the model object for the sake of efficiency. If boots is not specified, then we will use the same bootstrap count in the permutation test WQS regression runs as that specified in the model argument.

The arguments b1\_pos and rs should be consistent with the inputs chosen in the model object. The seed should ideally be consistent with the seed set in the model object for consistency, though this is not required.

wqs\_pt

#### Value

wqs\_pt returns an object of class wqs\_pt, which contains:

perm\_test List containing: (1) pval: permutation test p-value, (2) (linear WQS regres-

sion only) testbeta1: reference WQS coefficient beta1 value, (3) (linear WQS regression only) betas: Vector of beta values from each permutation test run, (4) (WQS GLM only) testpval: test reference p-value, (5) (WQS GLM only)

permpvals: p-values from the null models.

gwqs\_main Main gWQS object (same as model input).

gwqs\_perm Permutation test reference gWQS object (NULL if model family != "gaussian"

or if same number of bootstraps are used in permutation test WQS regression

runs as in the main run).

#### References

Day, D. B., Sathyanarayana, S., LeWinn, K. Z., Karr, C. J., Mason, W. A., & Szpiro, A. A. (2022). A permutation test-based approach to strengthening inference on the effects of environmental mixtures: comparison between single index analytic methods. Environmental Health Perspectives, 130(8).

Day, D. B., Collett, B. R., Barrett, E. S., Bush, N. R., Swan, S. H., Nguyen, R. H., ... & Sathyanarayana, S. (2021). Phthalate mixtures in pregnancy, autistic traits, and adverse childhood behavioral outcomes. Environment International, 147, 106330.

Loftus, C. T., Bush, N. R., Day, D. B., Ni, Y., Tylavsky, F. A., Karr, C. J., ... & LeWinn, K. Z. (2021). Exposure to prenatal phthalate mixtures and neurodevelopment in the Conditions Affecting Neurocognitive Development and Learning in Early childhood (CANDLE) study. Environment International, 150, 106409.

#### **Examples**

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wqs\_sim

WQS simulated dataset generator

#### **Description**

wqs\_sim generates a simulated dataset of mixture components, covariates, and outcomes based on an initial set of specifications.

#### Usage

```
wqs_sim(
  nmix = 10,
  ncovrt = 10,
 nobs = 500,
  ntruewts = 10,
  ntruecovrt = 5,
  vcov = 0,
  eps = 1,
  truewqsbeta = NULL,
  truebeta0 = NULL,
  truewts = NULL,
  truegamma = NULL,
  rnd_wqsbeta_dir = "none",
  seed = 101,
  q = 10,
  family = "gaussian"
)
```

#### **Arguments**

nmix Number of mixture components in simulated dataset.

ncovrt Number of covariates in simulated dataset.

Number of observations in simulated dataset.

ntruewts Number of mixture components that have a non-zero association with the out-

come (i.e., are not noise).

ntruecovrt Number of covariates that have a non-zero association with the outcome (i.e.,

are not noise).

vcov This parameter relates to the variance-covariance matrix of the simulated inde-

pendent variables (i.e., the m exposure mixture components and z covariates). This is either a variance-covariance matrix of dimensions (m + z) x (m + z) or a single value. If this is a single value, the variance- covariance matrix will have ones on the diagonal and that single value will be all the off-diagonal values. For example, if this input were 0.4 and there were two mixture components and no covariates, the variance-covariance matrix would be matrix(c(1, 0.4, 0.4, 1), nrow = 2, c(1, 0.4, 0.4, 1)). The default value is 0, giving a variance-covariance matrix

with variances of 1 and covariances of 0.

wqs\_sim

eps Dispersion parameter. If the family is "gaussian", this corresponds to the resid-

ual standard deviation. If the family is "binomial" or "poisson", this parameter is ignored. If the family is "negbin", this represents the "size" parameter of the negative binomial distribution (see the documentation for the rnbinom function

for more details).

truewqsbeta Simulated WQS beta\_1 value. If NULL, then this value will be randomly sam-

pled depending on the parameter rnd\_wqsbeta\_dir.

truebeta0 Simulated beta 0 value. If NULL, then this value will be randomly sampled

from a standard normal distribution.

truewts Simulated vector of mixture weights. If NULL, then this value will be randomly

sampled from a Dirichlet distribution with a vector of alpha values all equal to 1 (see the documentation for the extraDistr::rdirichlet function documentation for

more details).

truegamma Simulated gamma vector. If NULL, then this value will be randomly sampled

from a standard normal distribution.

rnd\_wqsbeta\_dir

Direction of randomly sampled truewqsbeta (if truewqsbeta = NULL). The options are "positive", "negative", or NULL. If "positive" or "negative", the truewqsbeta will be sampled from a standard half normal distribution in either of those respective directions. If NULL, then truewqsbeta will be sampled from a stan-

dard normal distribution.

seed Random seed.

q Number of quantiles.

family Family for the generative model creating the outcome vector. Options include

"gaussian" or gaussian(link = "identity") for a continuous outcome, "binomial" or binomial() with any accepted link function for a binary outcome, and finally for count outcomes this can be "poisson" or poisson(link="log") for the Poisson distributed outcome values, or "negbin" for negative binomial distributed

outcome values.

#### Value

wqs\_perm returns a list of:

weights Simulated weights.

coef Simulated beta coefficients.

Data Simulated dataset.

etahat predicted linear predictor (eta) values from the data generating model.

wqs Weighted quantile sum vector (quantile-transformed mixture components mul-

tiplied by weights).

modmat Model matrix.

Xq Quantile-transformed mixture components.

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#### **Examples**

```
# For these examples, we only run a GLM using the simulated dataset
# including the simulated WQS vector just to show that the user-specified
# coefficients for beta1 and beta0 are returned. An example of running
# the full permutation test WQS regression for the simulated dataset
# (for which the WQS vector would be determined by the model)
# with the "gaussian" family is shown as well.
wqsform<-formula(paste0("y~wqs+",paste(paste0("C",1:10),collapse="+")))</pre>
testsim_gaussian<-
  wqs_sim(truewqsbeta=0.2,truebeta0=-2,
          truewts=c(rep(0.15,5),rep(0.05,5)),family="gaussian")
Dat<-testsim_gaussian$Data
Dat$wqs<-testsim_gaussian$wqs</pre>
summary(glm(wqsform,data=Dat,family="gaussian"))$coef[1:2,]
perm_test_res <- wqs_full_perm(formula = wqsform, data = testsim_gaussian$Data,</pre>
                                mix_name = paste0("T", 1:10), q = 10, b_main = 5,
                                b_perm = 5, b1_pos = TRUE, b1_constr = FALSE,
                                niter = 4, seed = 16, plan_strategy = "multicore",
                                stop_if_nonsig = FALSE)
# Note: The default values of b_main = 1000, b_perm = 200, and niter = 200
# are the recommended parameter values. This example has a lower b_main,
# b_perm, and niter in order to serve as a shorter example run.
testsim_logit<-
  wqs_sim(truewqsbeta=0.2,truebeta0=-2,
          truewts=c(rep(0.15,5), rep(0.05,5)), family="binomial")
Dat<-testsim_logit$Data
Dat$wqs<-testsim_logit$wqs</pre>
summary(glm(wqsform,data=Dat,family="binomial"))$coef[1:2,]
```

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